



Braking effect (velocity strengthening) of Kaolinite under intermediate slip velocities.

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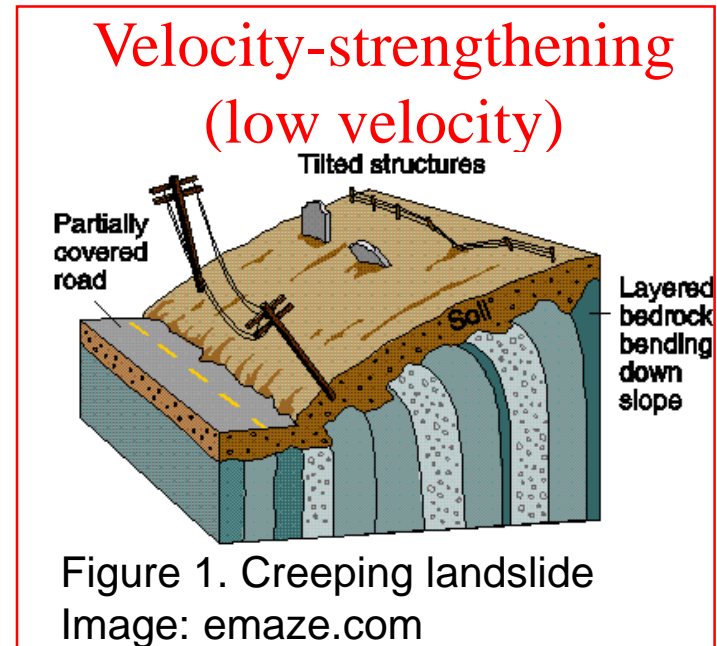
1. Creeping landslide???

- Creep is the slow downslope movement of material under gravity. It generally occurs over large areas. (shallow fault zones)

| Velocity class | Description | Velocity (mm/s) | Typical velocity |
|----------------|-----------------|----------------------|--------------------------|
| 7 | Extremely rapid | 5×10^3 | >5m/s |
| 6 | Very rapid | 5×10^1 | 3 m/min - 5m/s |
| 5 | Rapid | 5×10^{-1} | 1.8 m/h – 3 m/min |
| 4 | Moderate | 5×10^{-3} | 13m/month – 1,8m/h |
| 3 | Slow | 5×10^{-5} | 1.6 m/year – 13m/ month |
| 2 | Very slow | 5×10^{-7} | 16 mm/ year - 1.6 m/year |
| 1 | Extremely slow | $< 5 \times 10^{-7}$ | <16mm/year |

Table: International Union of Geological Sciences Working Party on the World Landslide Inventory velocity classes (after IUGS 1995)

Mechanism???



- Slope angle ($< 20^\circ$ (Seda Cellek, 2020))
- Water (groundwater, rainfall)
- Material of rock
- Earthquake
- ...

- What is steady state:
 - Velocity weakening (SVW)?
 - Velocity Strengthening (SVS)?
- Frictional resistance increases with sliding velocity

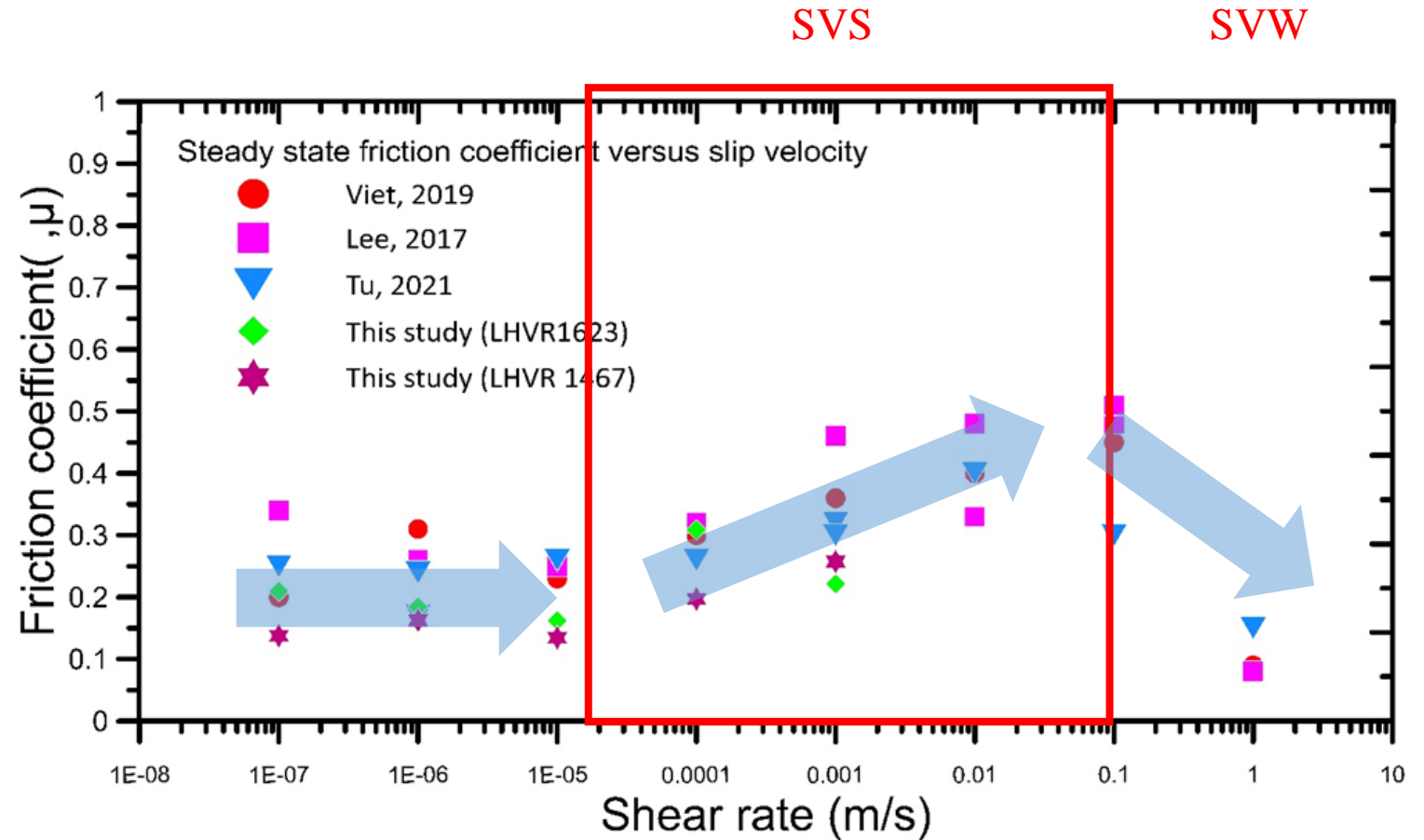


Figure 2. The steady-state apparent friction coefficients under different slip rates

2. Review paper

Newmark proposed a displacement-based analysis method to **calculate the permanent displacement** of artificial embankments and **natural slopes encountered seismic force**.

If earthquake acceleration $> a_c$ (critical acceleration), the block will slide down the sliding surface

After the block slide low ($a < a_c$),

velocity start to decrease

If the velocity of block stops ($v = 0$), the block stops sliding

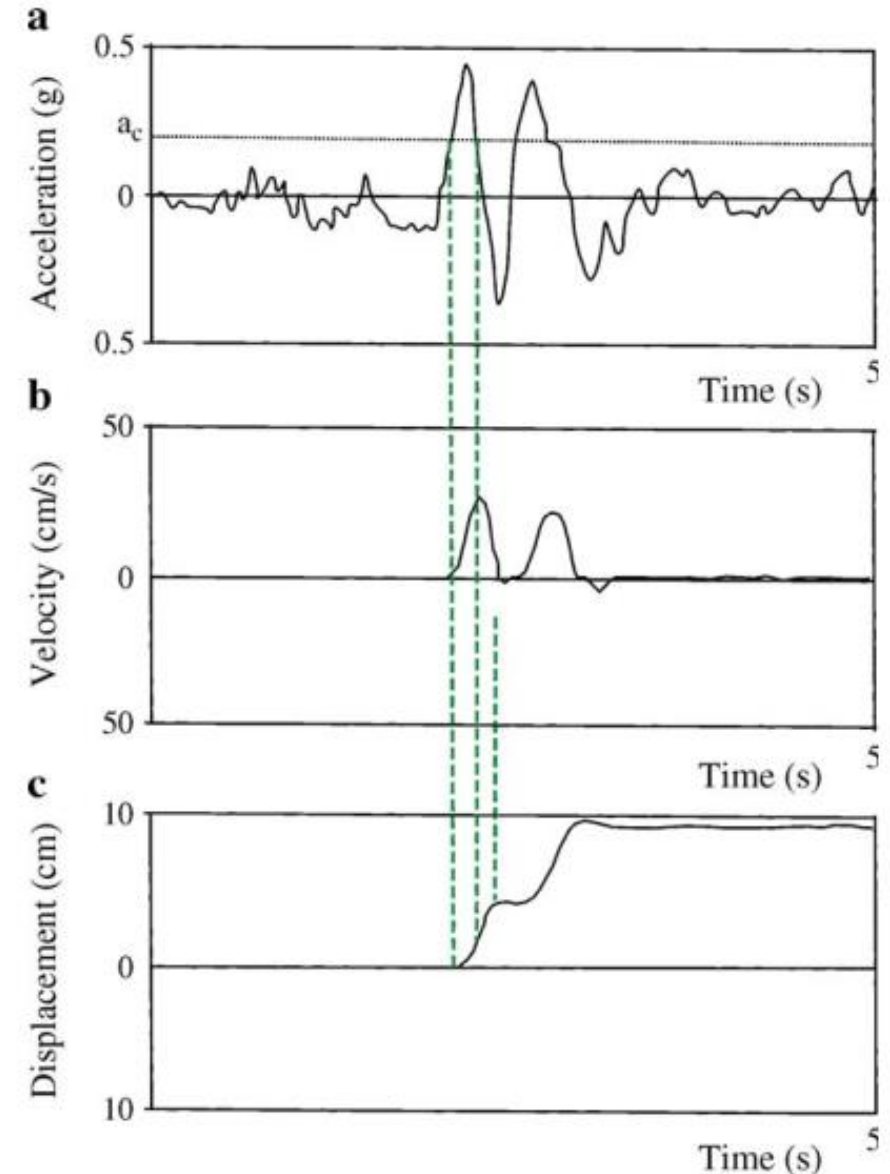


Figure 3. Double-integration approach of Newmark displacement analysis

3. Objective

At low velocity:

1. Height watertable above failure surface

2. Friction coefficient

→ Creeping landslide

- Purpose of research:

Contribution: validate and compare data with previous studies

Explanation mechanism velocity-strengthening

Applications, predictions and warnings landslides

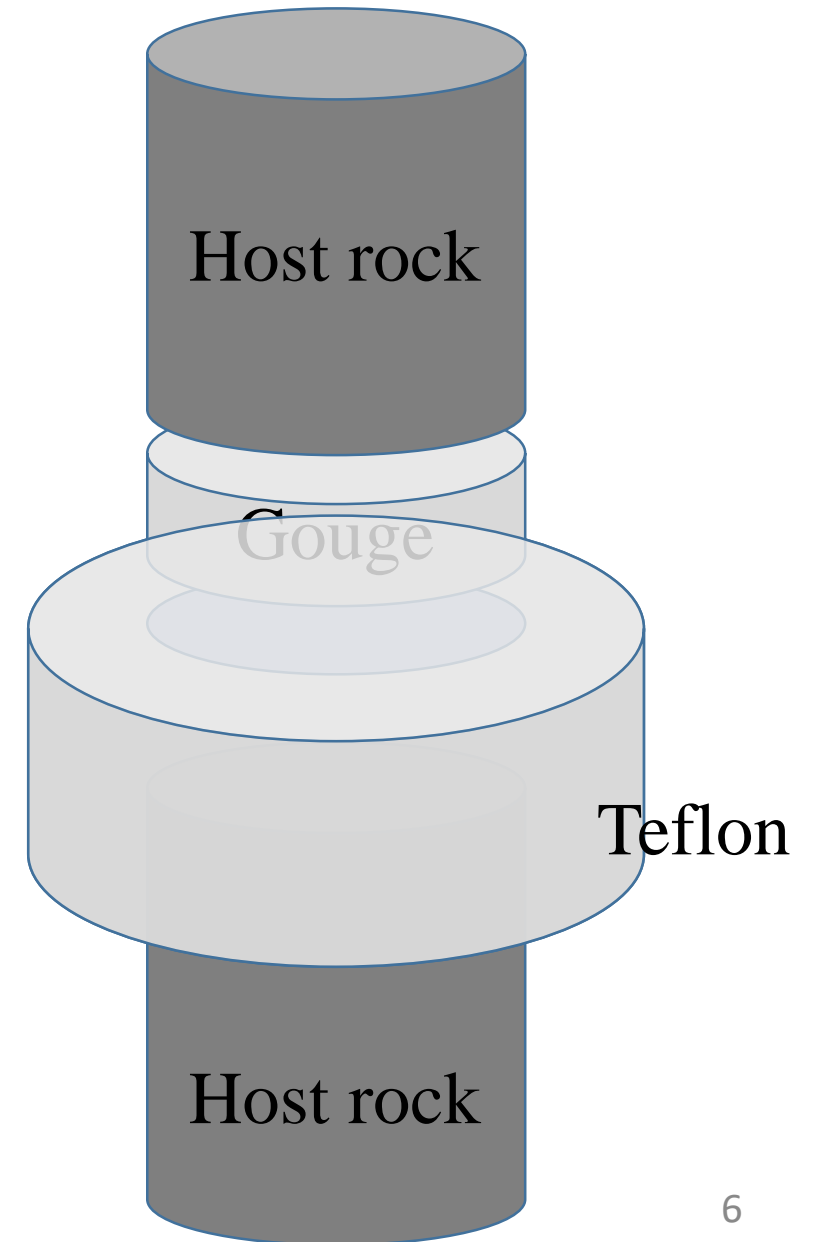
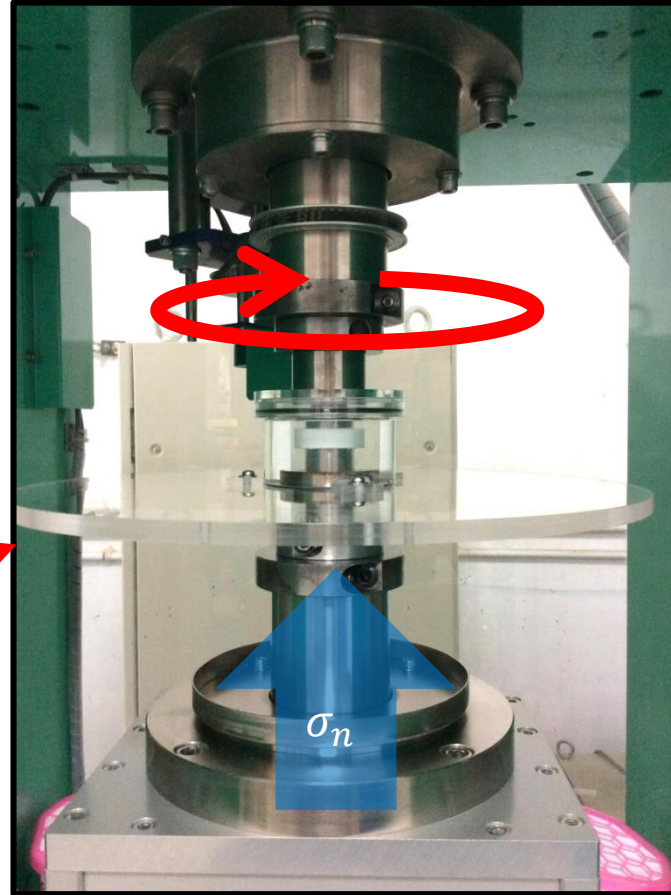
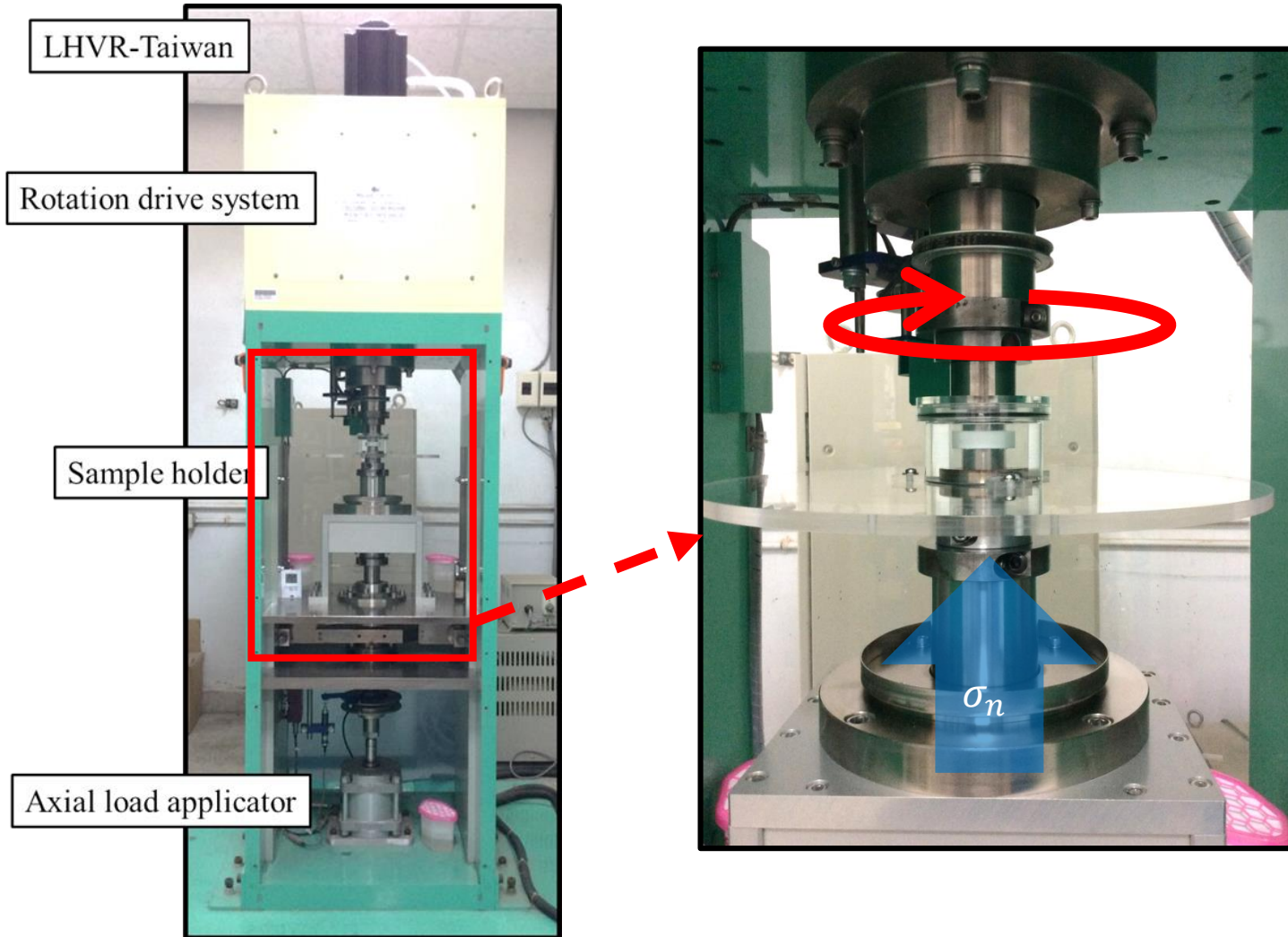
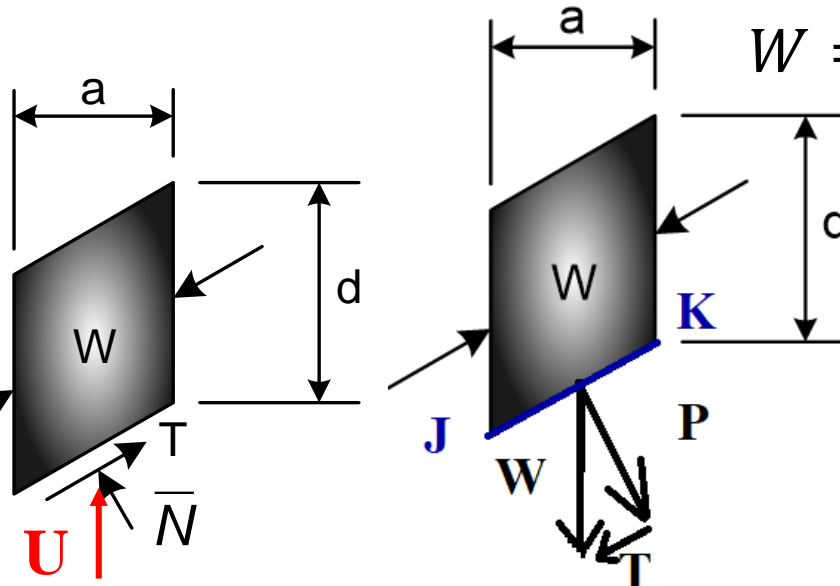
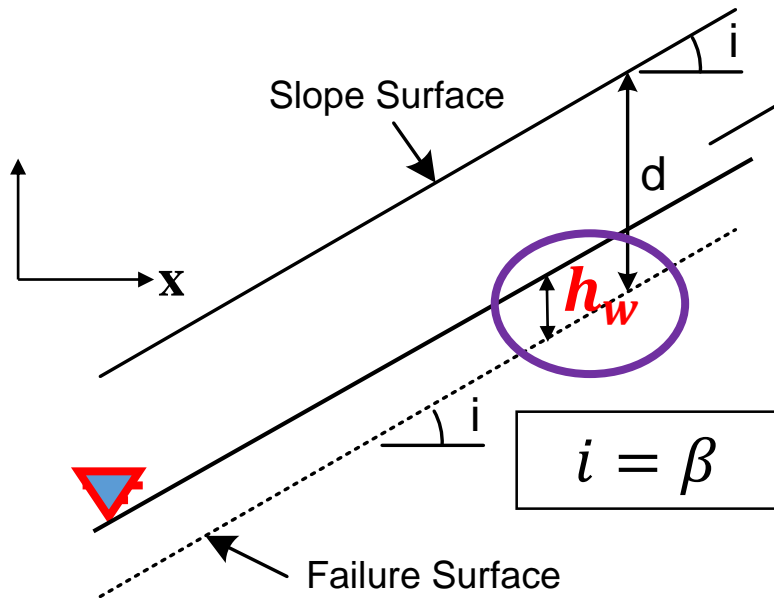


Figure 4. The rotary-shear low- to high-velocity frictional testing apparatus at the National Central University of Taiwan. (Lee, 2017)

Infinite Slopes in Soils with Parallel Seepage

a : the slice of width
 h : height soil
 γ_w : unit weight water
 γ_{sub} : unit weight soil
 i : slope angle



$$W = a \cdot d \cdot \gamma_{sub}$$

Shear component of weight:

$$T = W \cdot \sin \beta$$

$$T = a \cdot d \cdot \gamma_{sub} \cdot \sin \beta$$

Normal component of weight:

$$P = W \cdot \cos \beta$$

$$P = a \cdot d \cdot \gamma_{sub} \cdot \cos \beta$$

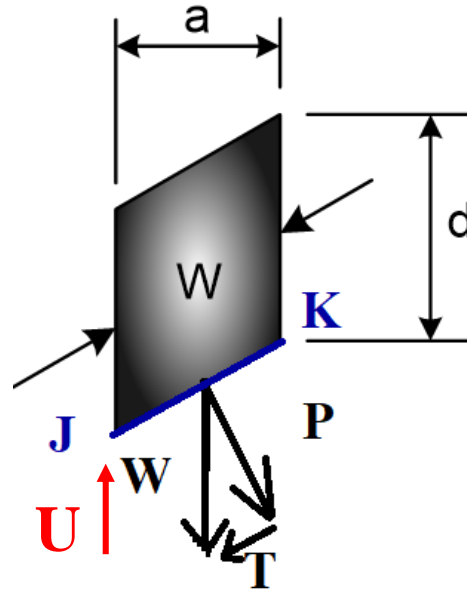
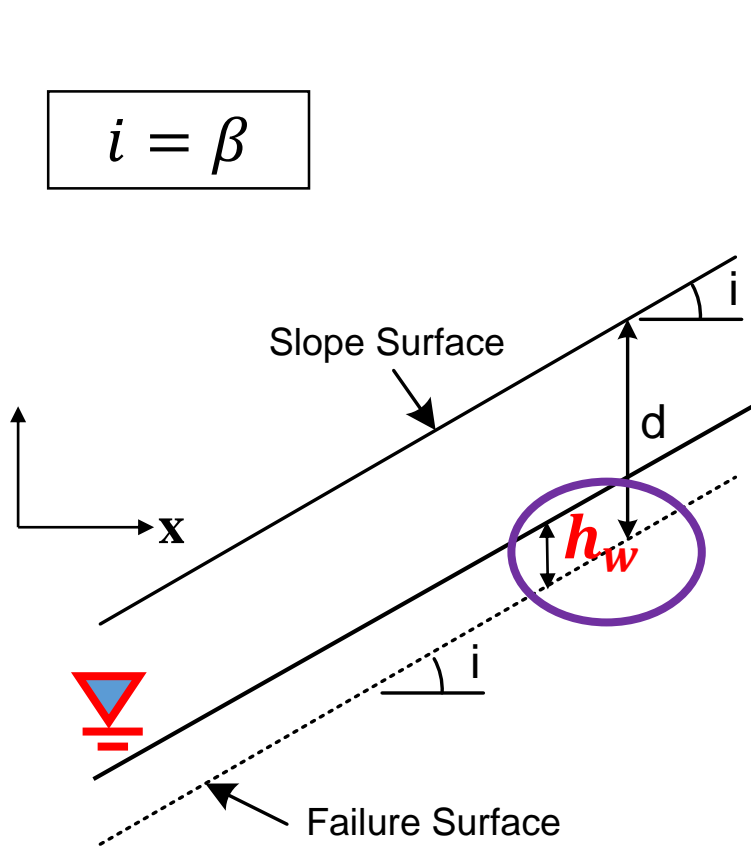
Shear stress:

$$\tau = \frac{T}{JK} = \frac{a \cdot d \cdot \gamma_{sub} \cdot \sin \beta}{\frac{a}{\cos \beta}} = \gamma_{sub} \cdot d \cdot \sin \beta \cdot \cos \beta$$

Normal stress:

$$\sigma = \frac{P}{JK} = \frac{a \cdot d \cdot \gamma_{sub} \cdot \cos \beta}{\frac{a}{\cos \beta}} = \gamma_{sub} \cdot d \cdot \cos^2 \beta$$

h_w : height water
 above failure surface

Prove that FS varies with groundwater

h_w : height water
above failure surface

- Normal component of water weight:

$$P_w = \gamma_w \cdot a \cdot h_w \cdot \cos \beta$$

- Pore water pressure on JK

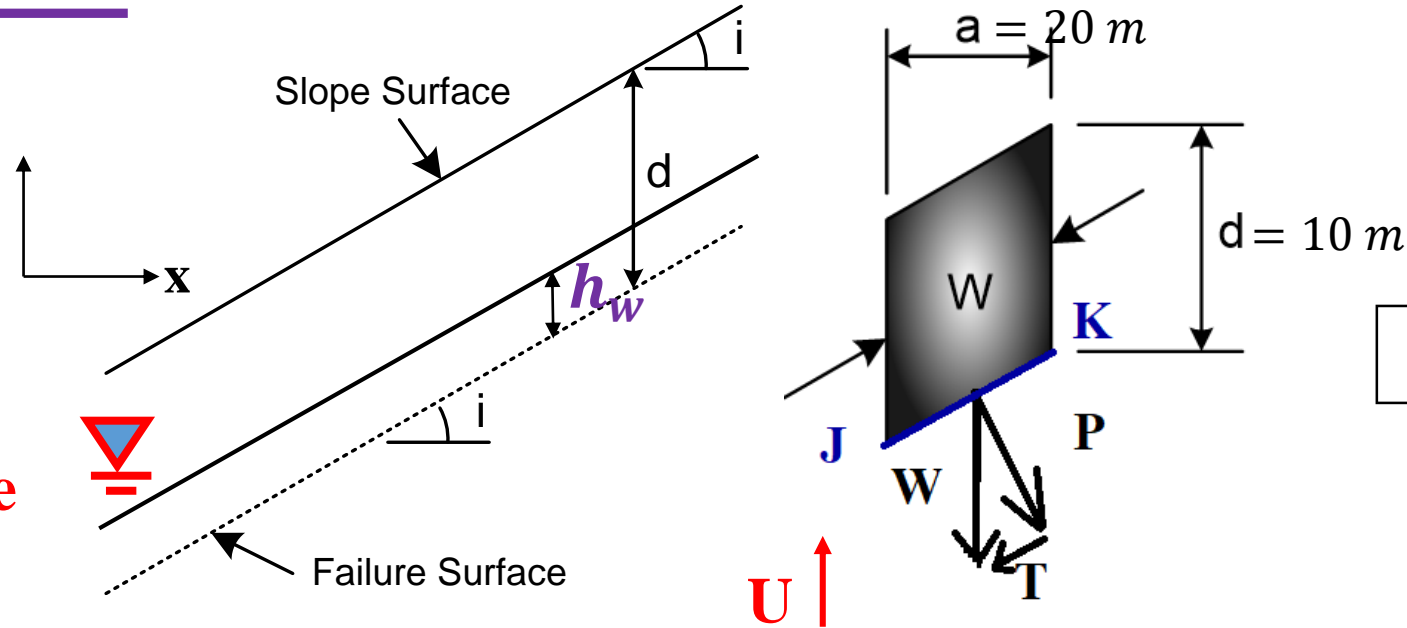
$$U = \frac{\gamma_w \cdot a \cdot h_w \cdot \cos \beta}{a}$$

$$= \gamma_w \cdot h_w \cdot \cos^2 \beta$$

Factor of safety:

$$FS = \frac{C' + (\sigma - U) \tan \phi}{\tau} = \frac{C' + (\gamma_{sub} \cdot d \cdot \cos^2 \beta - \gamma_w \cdot h_w \cdot \cos^2 \beta) \tan \phi}{\gamma_{sub} \cdot d \cdot \sin \beta \cdot \cos \beta}$$

Assumption



**$h_w = 7.5 \rightarrow 7.85 \text{ m}$:
height water above
failure surface**

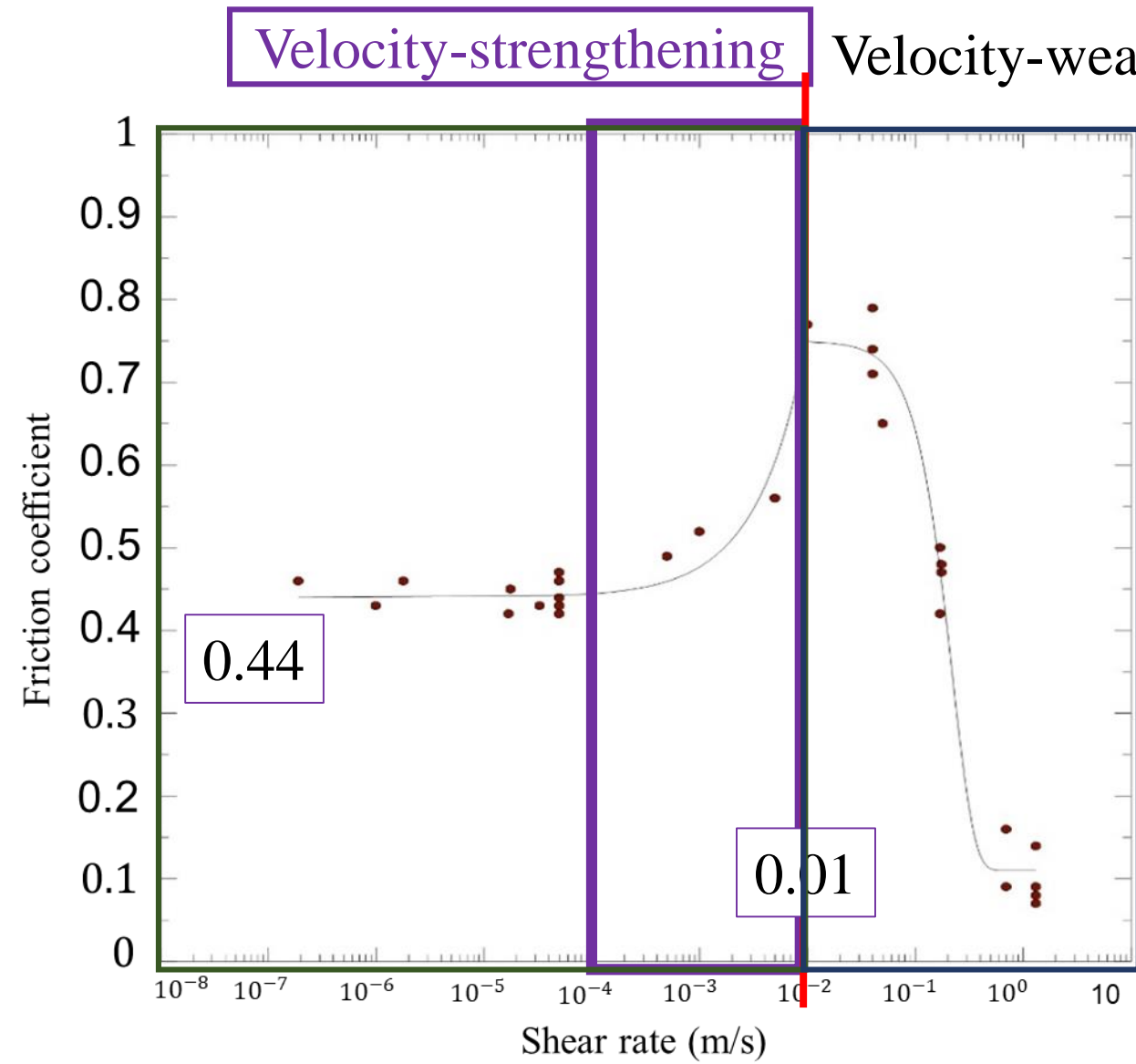
$$\rho_{sub} = 2000 \frac{kg}{m^3} \rightarrow \gamma_{sub} = 2000 * 9.81 = 19620 \frac{kg}{m^2 * s^2}$$

$$\phi = 30^\circ, C' = 0$$

$$\gamma_w = 9810 \frac{kg}{m^2 * s^2}$$

The direction of groundwater flow is parallel to the slope

Apply equation to calculate friction coefficient from velocity



Velocity-dependent friction law:

$$\mu(V) \begin{cases} = 0.44 + 22.47V^{0.93} & , V < 0.01 \text{ m/s} \\ = 0.11 + (0.75 - 0.11) \exp\left(\frac{-V^{2.13}}{0.04}\right) & , V > 0.01 \text{ m/s} \end{cases}$$

(Ferri et al., 2011)

Acceleration

$$-(m_{sub} + m_w) * acceleration = Resistance\ force - Driving\ force$$

$$acceleration = - \frac{Resistance\ force - Driving\ force}{(m_{sub} + m_w)}$$

weight

$$m_w = \gamma_w * d_w * a$$

$$m_{sub} = \gamma_{sub} * (d - d_w) * a$$

Integrate with time \rightarrow velocity (v) \rightarrow displacement (d)

1. Introduction

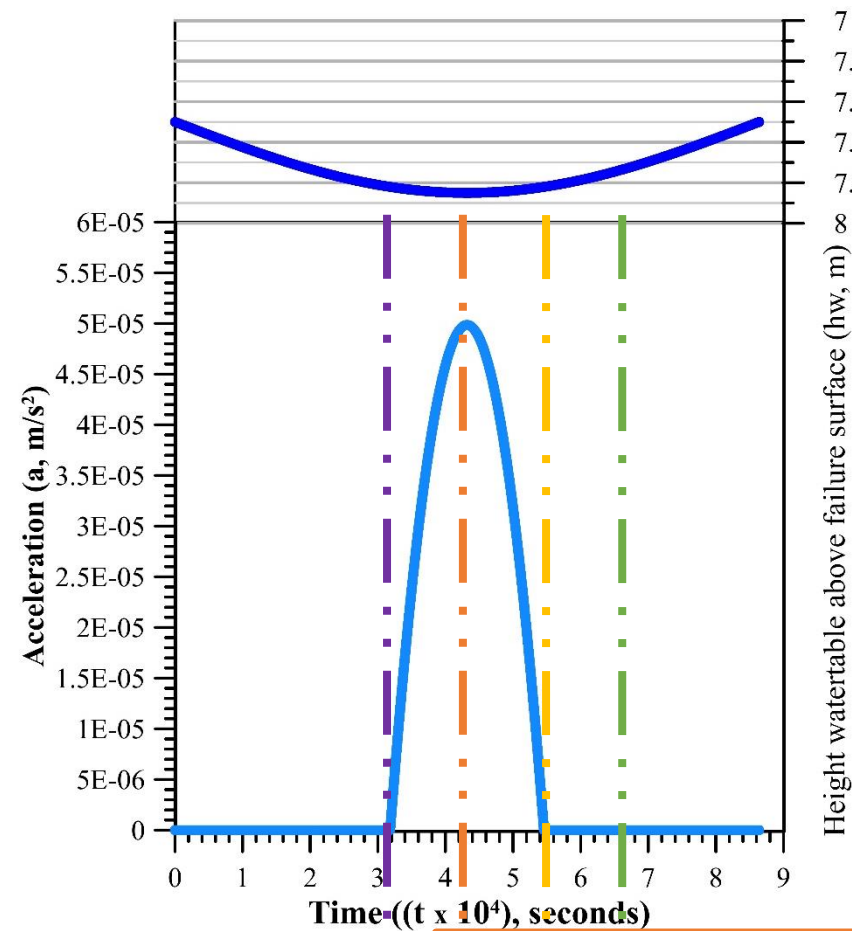
2. Methodology

3. Results

4. Discussion

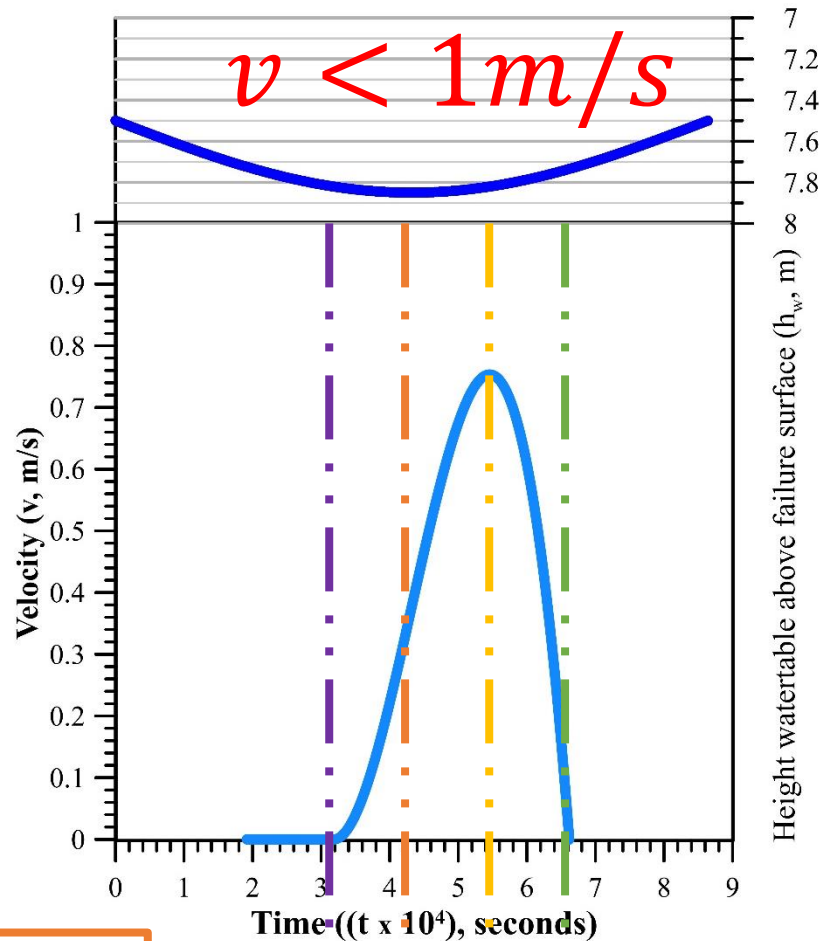
$$i = 15^\circ, h_w = 7.5 \text{ to } 7.85 \text{ m}, \mu = 0.44$$

Integrate with time



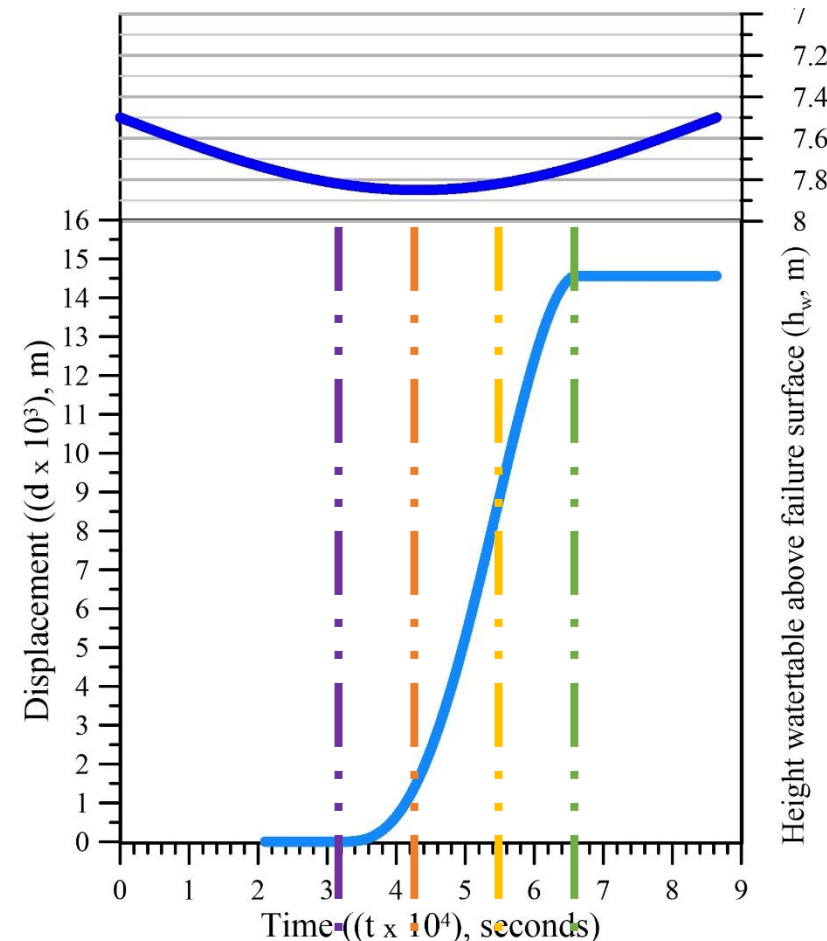
$t = 43200$ seconds

$t = 31825$ seconds



$t = 66183$ seconds

$t = 54575$ seconds



Implementing Processes

$$t_0 = \dots$$

$$\mu_0 = 0.44$$

$$h_{w0} = \dots, FS_0 = 1, a_0 = 0, v_0 = 0$$

Step 1

$$t_1 = t_0 + \Delta t$$

$$\mu_1 = 0.44$$

$$h_{w1} = \dots, FS_1 = \dots, a_1 = \dots, v_1 = \dots$$

$$\Rightarrow \mu_2 = \dots$$

$$\mu(V) \begin{cases} = 0.44 + 22.47V^{0.93} & , V < 0.01 \text{ m/s} \\ = 0.11 + (0.75 - 0.11) \exp\left(\frac{-V^{2.13}}{0.04}\right) & , V > 0.01 \text{ m/s} \end{cases}$$

Step 2

$$t_2 = t_1 + \Delta t$$

From $\mu_2 = \dots,$

$$h_{w2} = \dots, FS_2 = \dots, a_2 = \dots, v_2 = \dots$$

$$\Rightarrow \mu_3 = \dots$$

$$\Rightarrow \mu_3 = \dots$$

Example

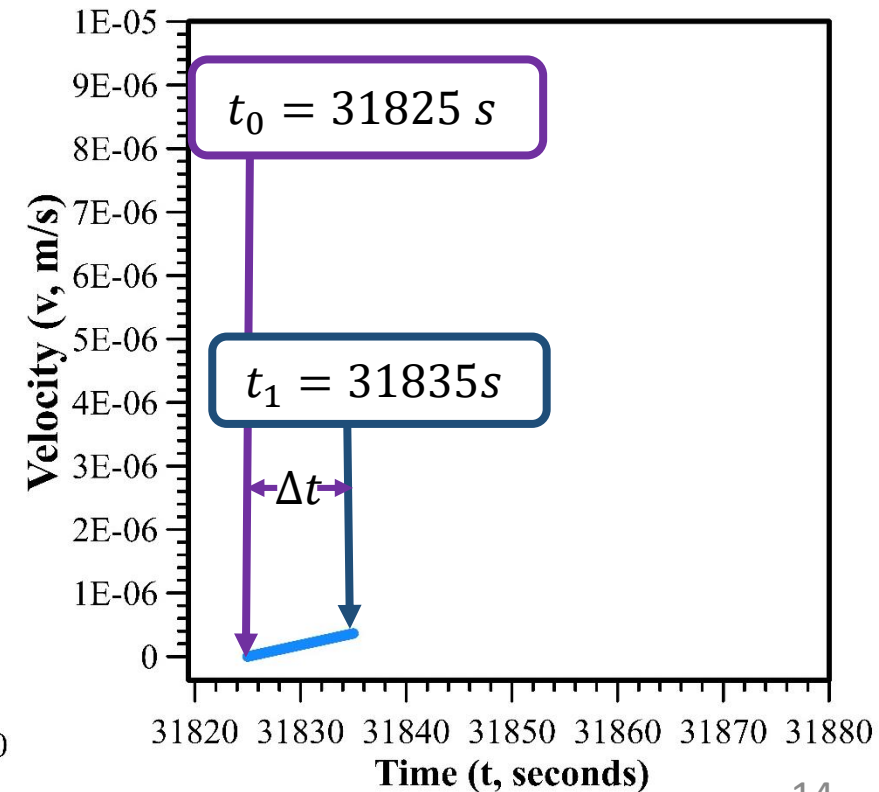
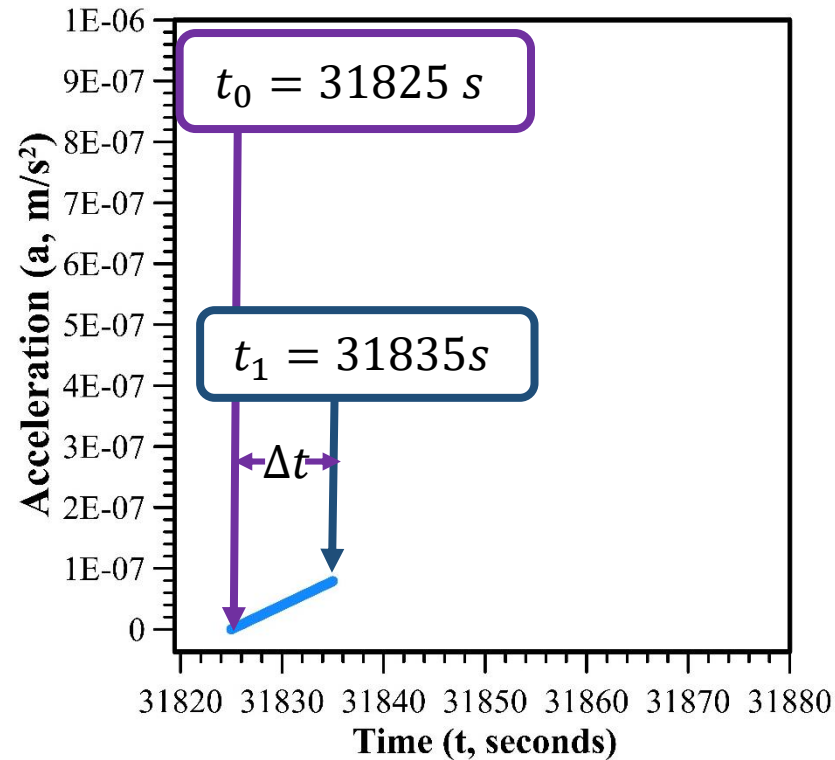
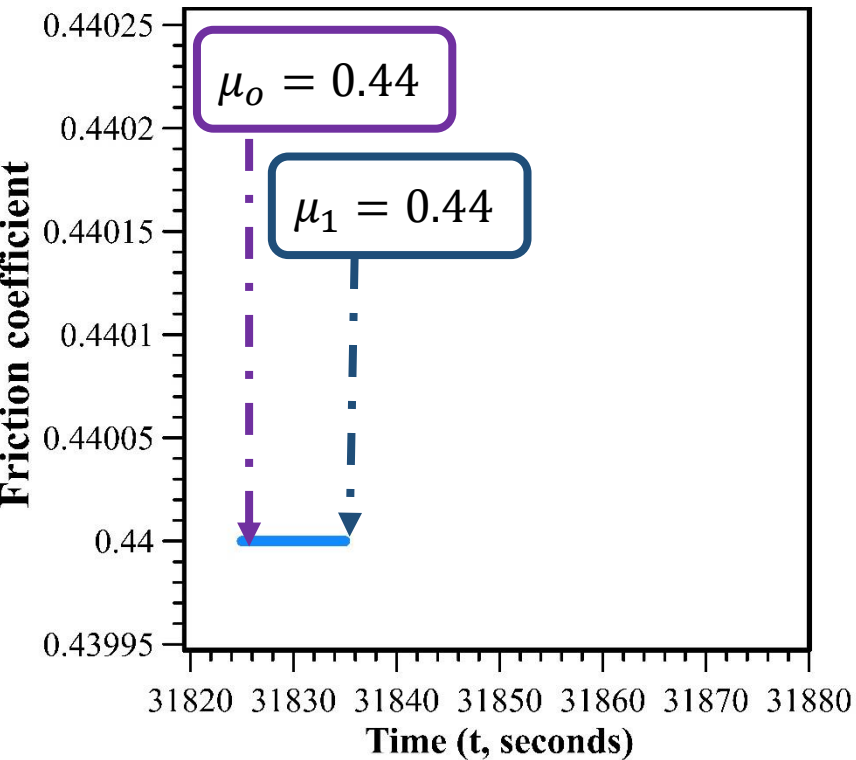
$$i = 15^\circ, h_w = 7.5 \text{ to } 7.85 \text{ m}, \Delta t = 10 \text{ s}$$

t_0

$\Delta t = 10 \text{ seconds}$

Step 1

$$t_1 = t_0 + \Delta t$$



Implementing processes

$t_0 = 31825 \text{ seconds}$

Step 1

$t_1 = t_0 + \Delta t$
 $= 31835 \text{ seconds}$

$\Rightarrow \mu_2 = 0.440023$

$\mu_0 = 0.44$

$h_{w0} = 7.82049 \text{ m}, FS_0 = 1,$

$a_0 = 0, v_0 = 0$

$\mu_1 = 0.44$

$h_{w1} = 7.82054 \text{ m}, FS_1 = 0.9999,$

$a_1 = 7.9037 \cdot 10^{-8} \text{ m/s}^2,$

$v_1 = 3.6316 \cdot 10^{-7} \text{ m/s}$

$$\mu(V) \begin{cases} = 0.44 + 22.47V^{0.93} & , V < 0.01 \text{ m/s} \\ = 0.11 + (0.75 - 0.11) \exp\left(\frac{-V^{2.13}}{0.04}\right) & , V > 0.01 \text{ m/s} \end{cases}$$

$\Rightarrow \mu_2 = 0.440023$

1. Introduction

2. Methodology

3. Results

4. Discussion

From $\mu_2 = 0.440023$ find acceleration and velocity next t_2

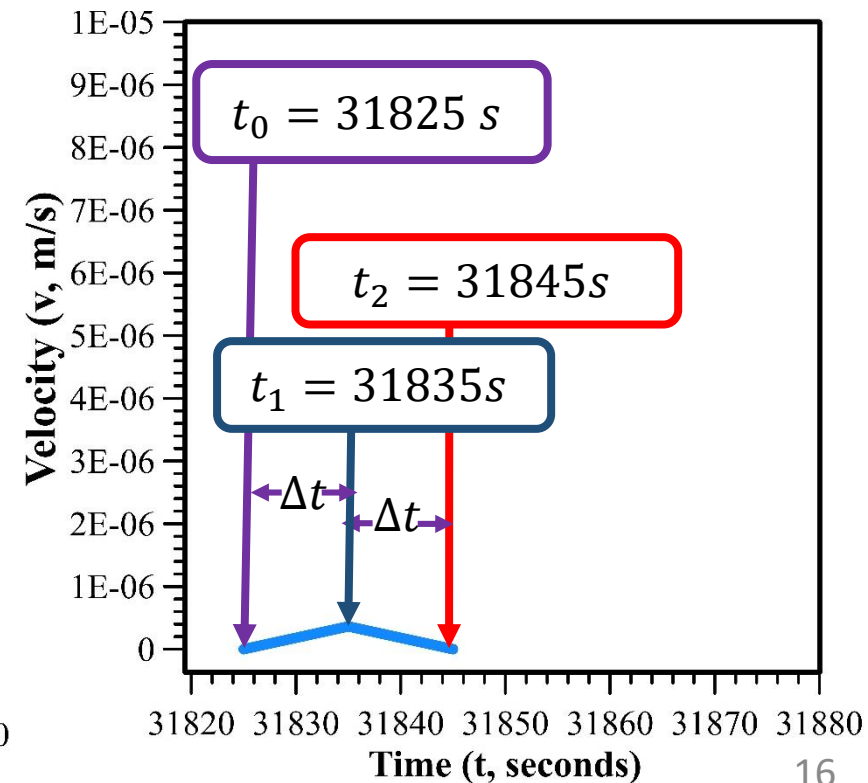
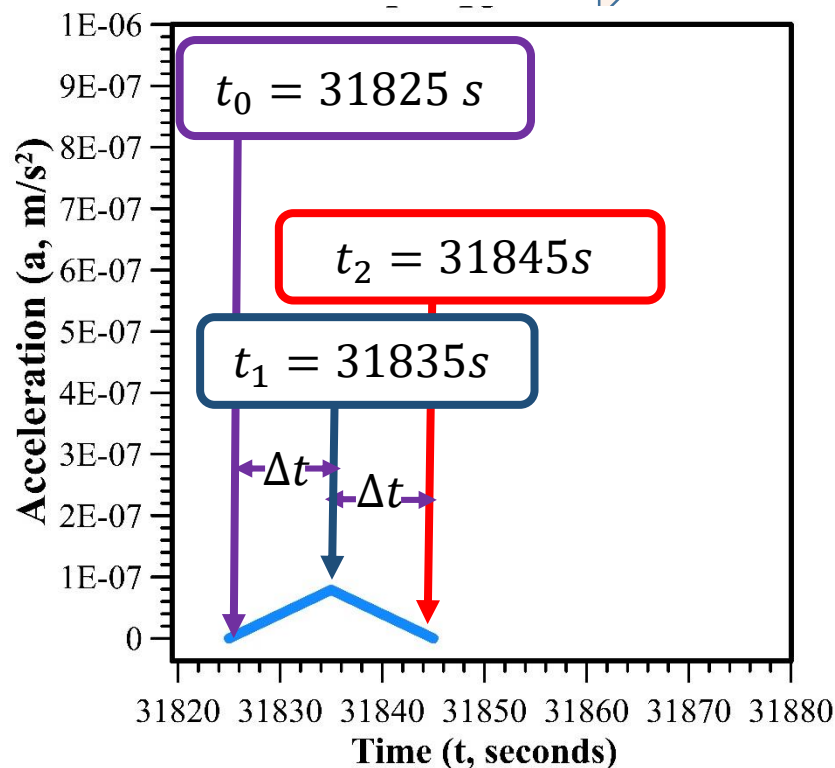
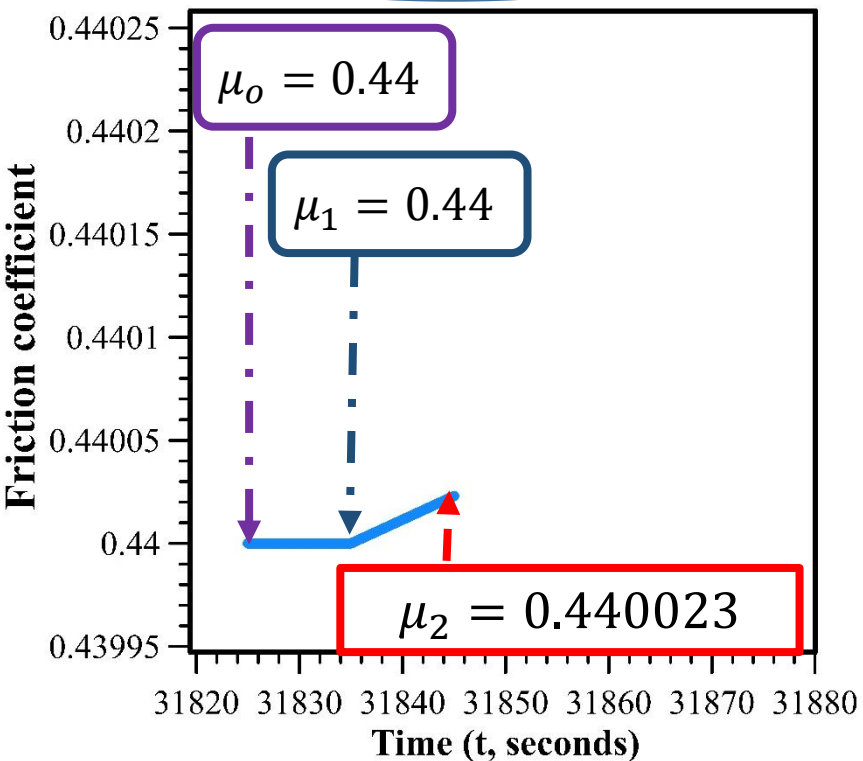
Step 1

t_1

$\Delta t = 10 \text{ seconds}$

Step 2

$t_2 = t_1 + \Delta t$



Implementation process

Step 1

t_1

$$\Rightarrow \mu_2 = 0.440023$$

Step 2

t_2

$$\Rightarrow \mu_3 = 0.44$$

$$\mu_1 = 0.44$$

$$h_{w1} = 7.82054 \text{ m}, FS_1 = 0.9999,$$

$$a_1 = 7.9037 \cdot 10^{-8} \text{ m/s}^2,$$

$$v_1 = 3.6316 \cdot 10^{-7} \text{ m/s}$$

From μ_2

$$h_{w2} = 7.82059 \text{ m}, FS_2 = 1.00004,$$

$$a_2 = 0 \text{ m/s}^2, v_2 = 0 \text{ m/s}$$

$$\mu(V) \begin{cases} = 0.44 + 22.47V^{0.93} & , V < 0.01 \text{ m/s} \\ = 0.11 + (0.75 - 0.11) \exp\left(\frac{-V^{2.13}}{0.04}\right) & , V > 0.01 \text{ m/s} \end{cases}$$

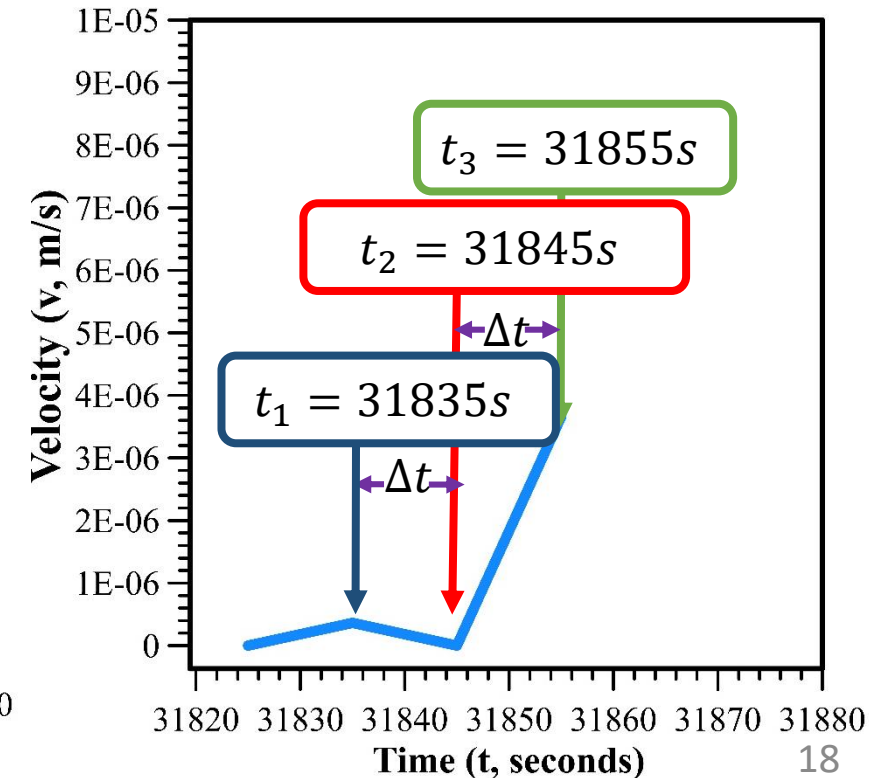
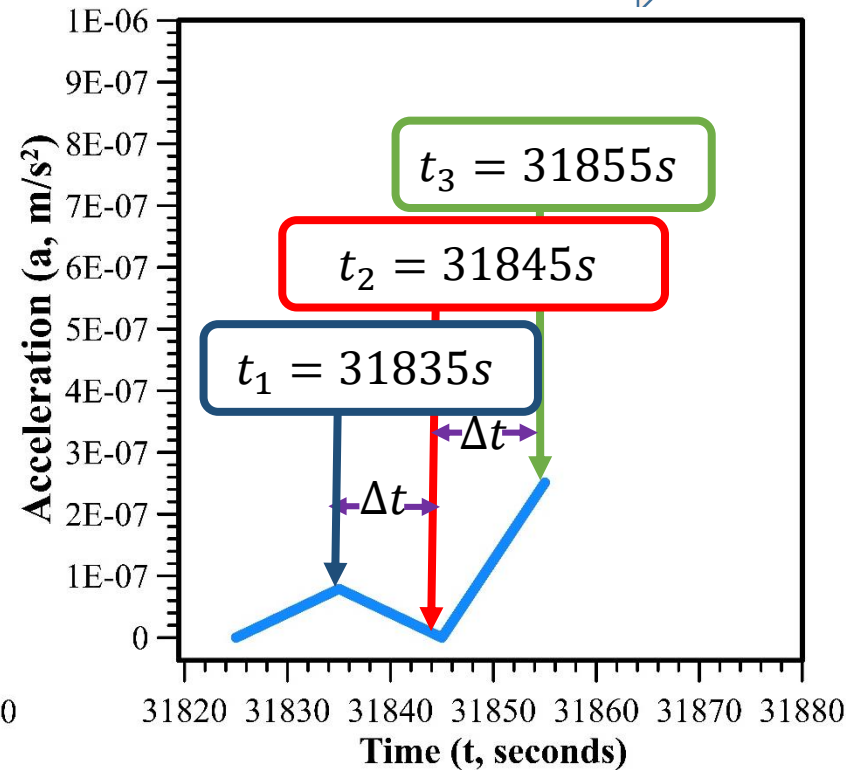
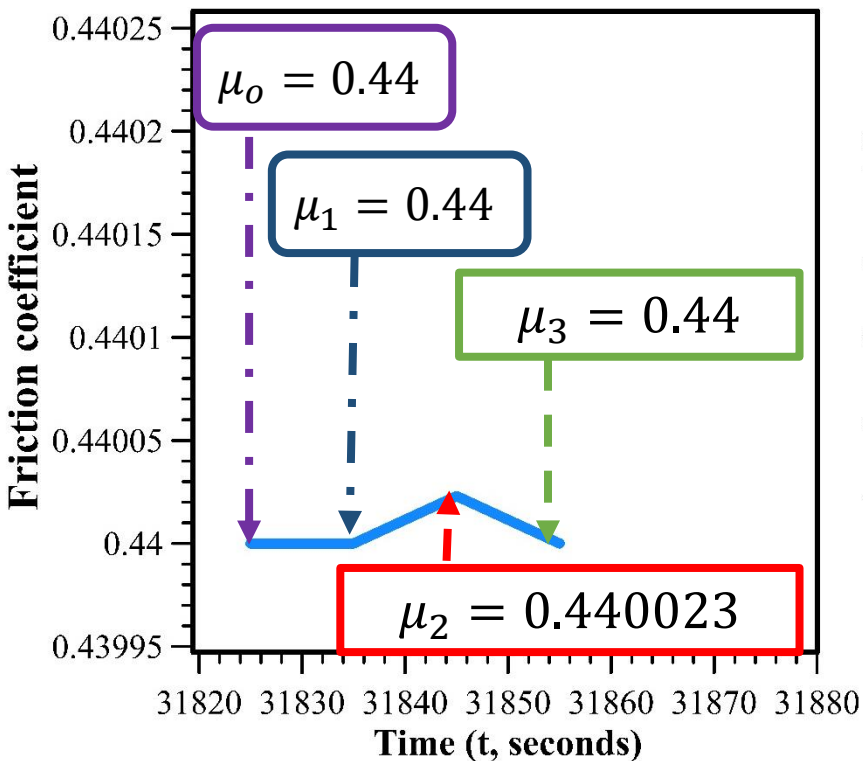
$$\Rightarrow \mu_3 = 0.44$$

From $\mu_3 = 0.44$ find acceleration and velocity next t_3

Step 2
 t_2

$\Delta t = 10 \text{ seconds}$

Step 3
 t_3



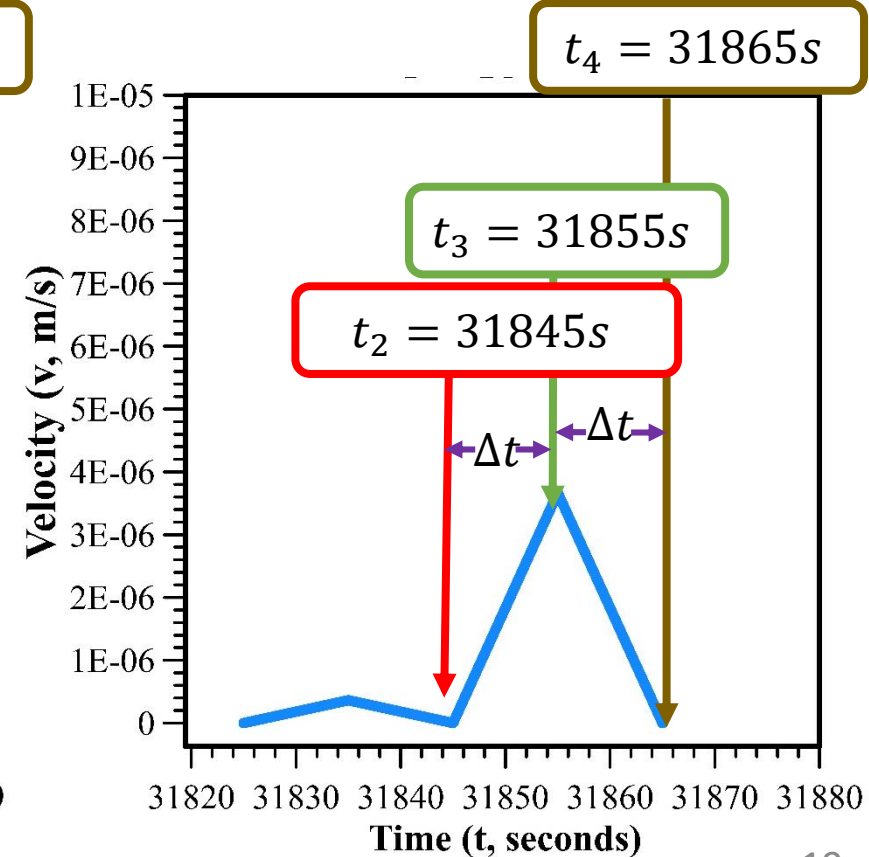
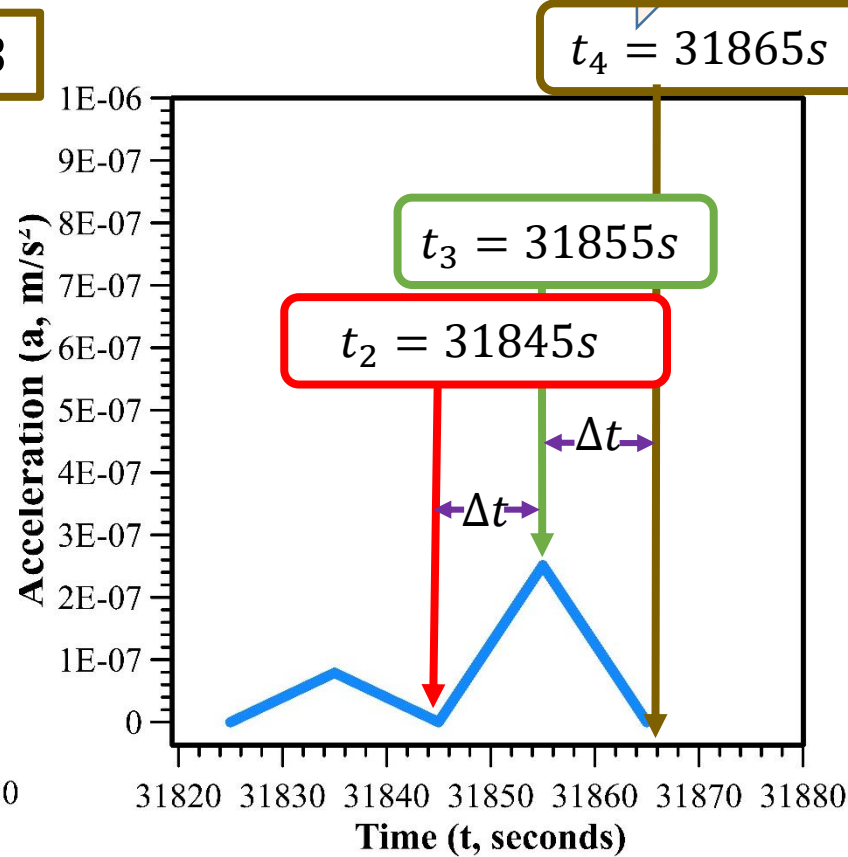
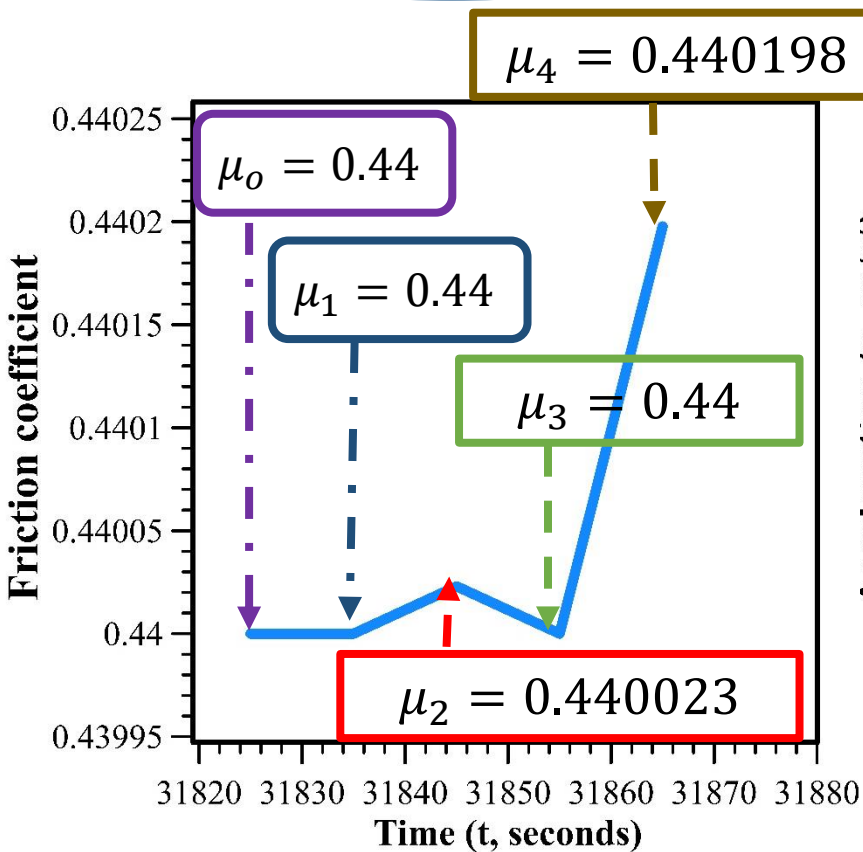
1. Introduction > 2. Methodology > **3. Results** > 4. Discussion

From $\mu_4 = 0.440198$ find acceleration and velocity next t_4

Step 3
 t_3

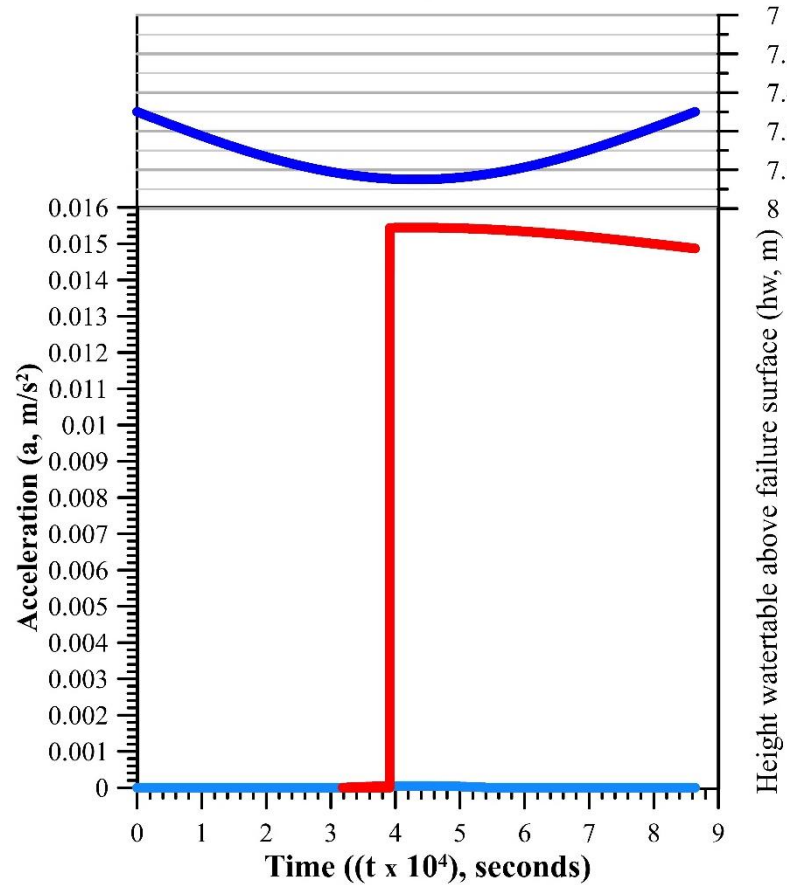
$\Delta t = 10 \text{ seconds}$

Step 4
 t_4



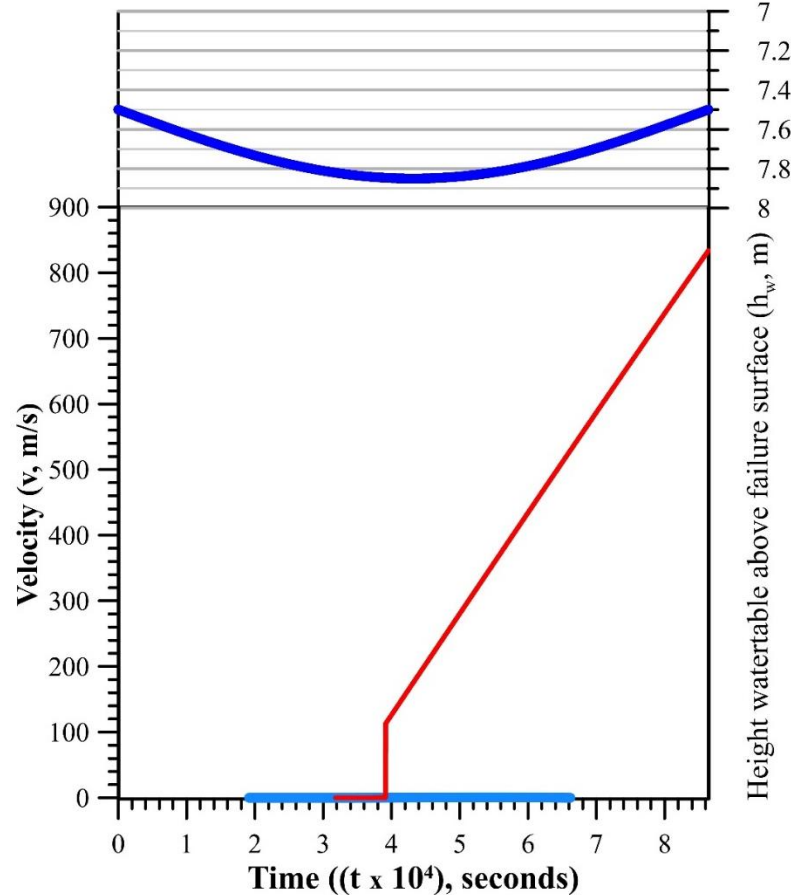
$$i = 15^\circ, h_w = 7.5 \text{ to } 7.85 \text{ m}, \Delta t = 10 \text{ s}$$

Acceleration - time

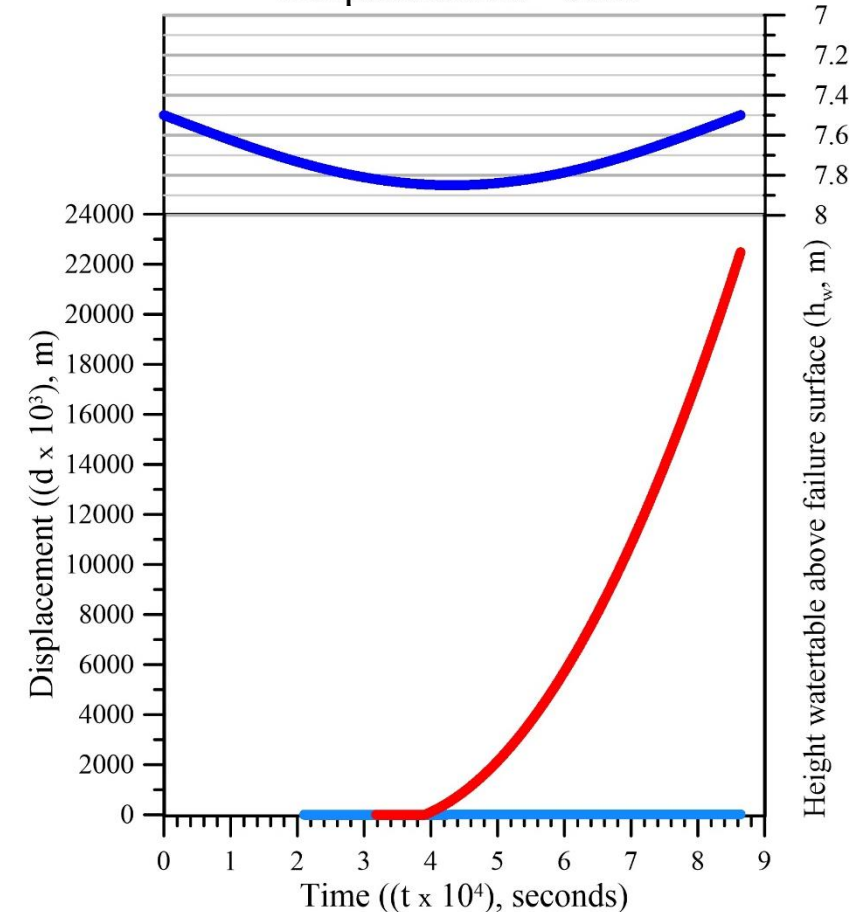


- acceleration from constant friction coefficient
- acceleration from change friction coefficient
- h_w

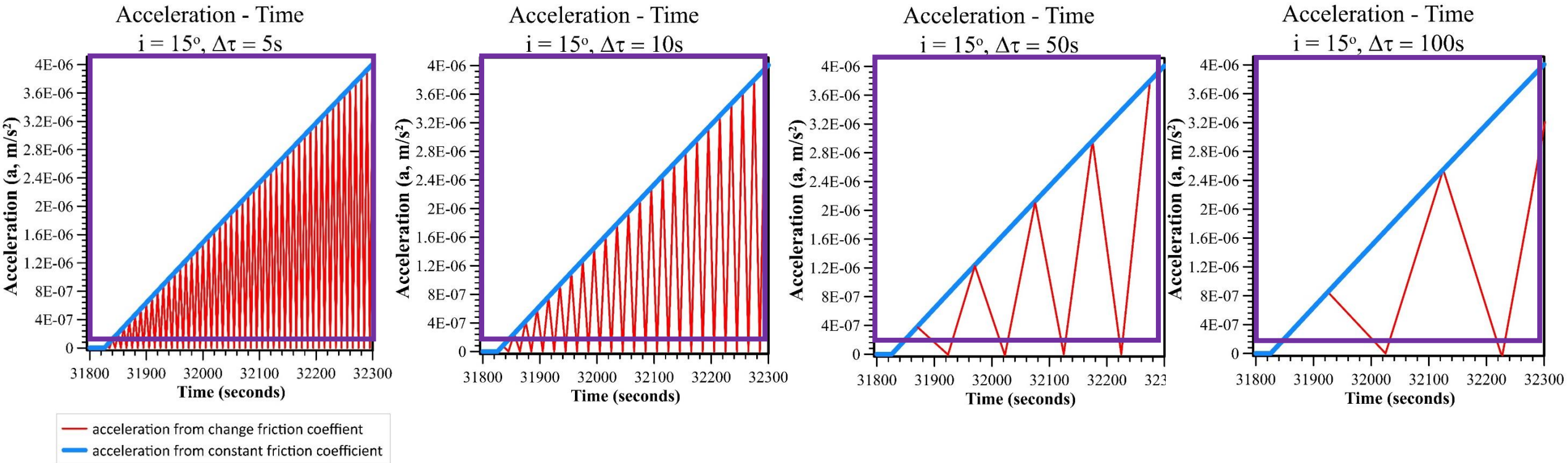
Velocity - time



Displacement - time



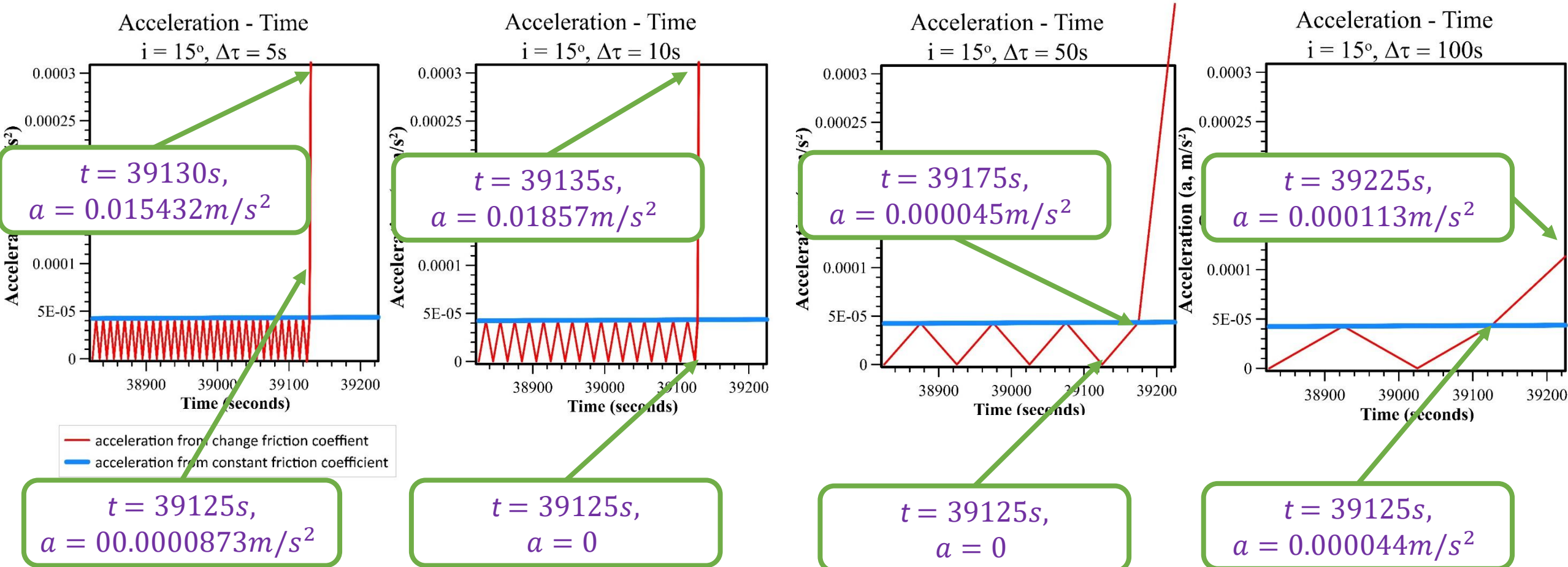
Acceleration with different Δt



Acceleration like figure zigzag

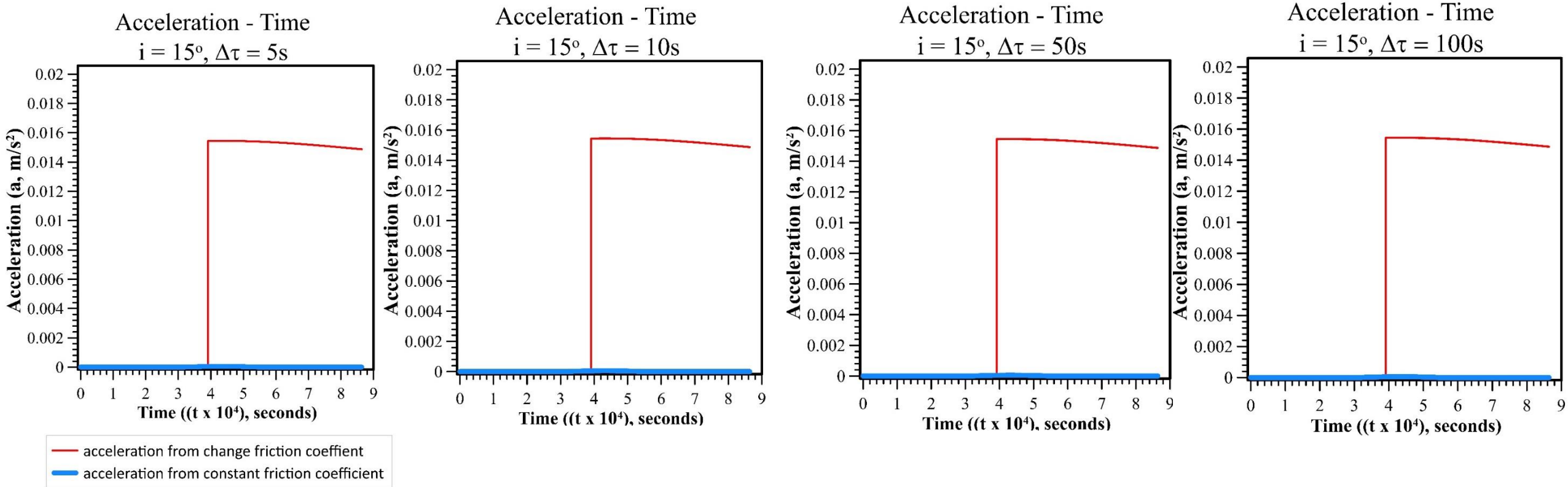
Acceleraton from change friction coefficient is limited by acceleration from constant friction coefficient

Acceleration with different Δt



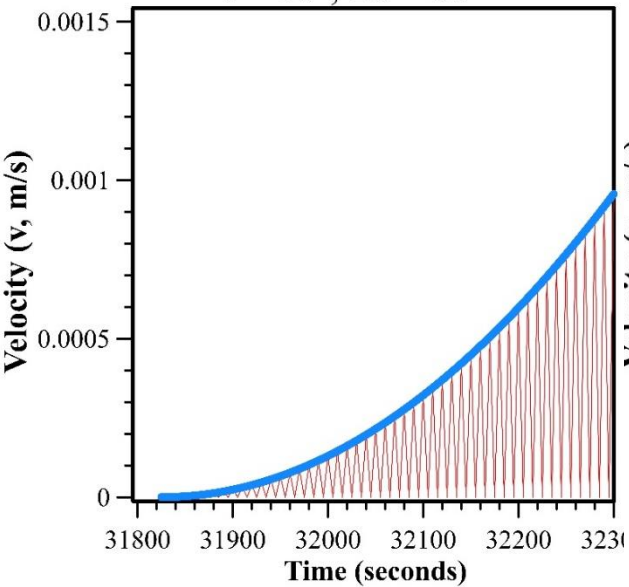
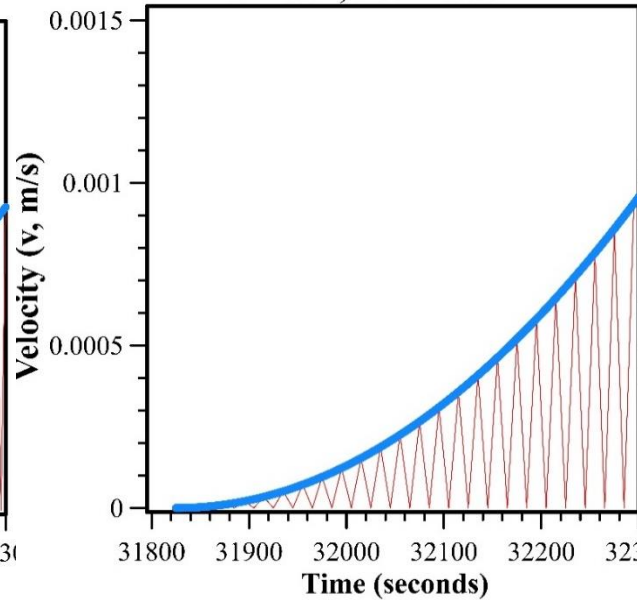
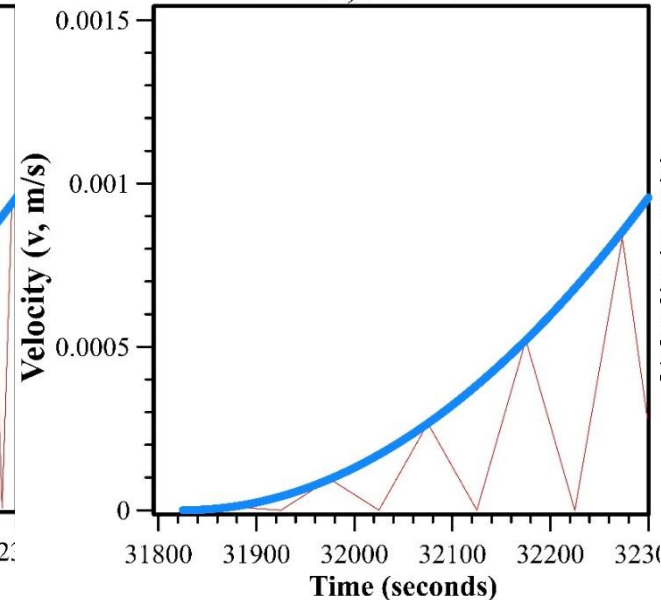
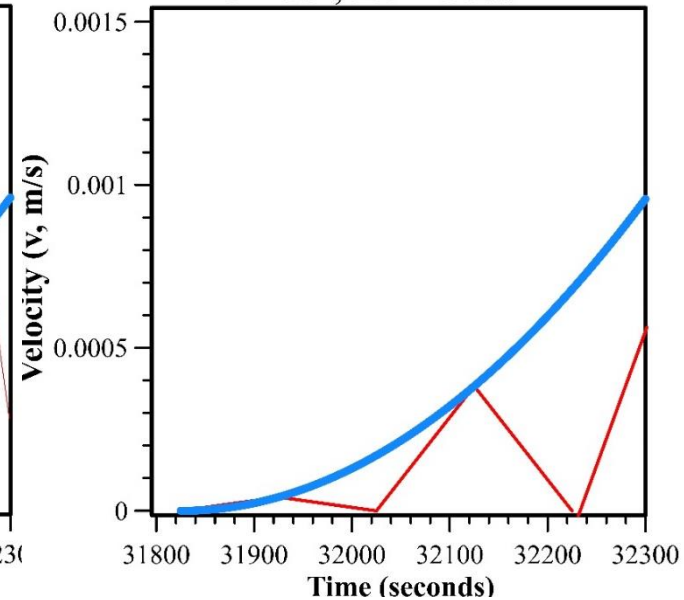
Acceleration changes slightly before sudden acceleration

Acceleration with different Δt



Acceleration of different Δt is similar

Velocity with different Δt

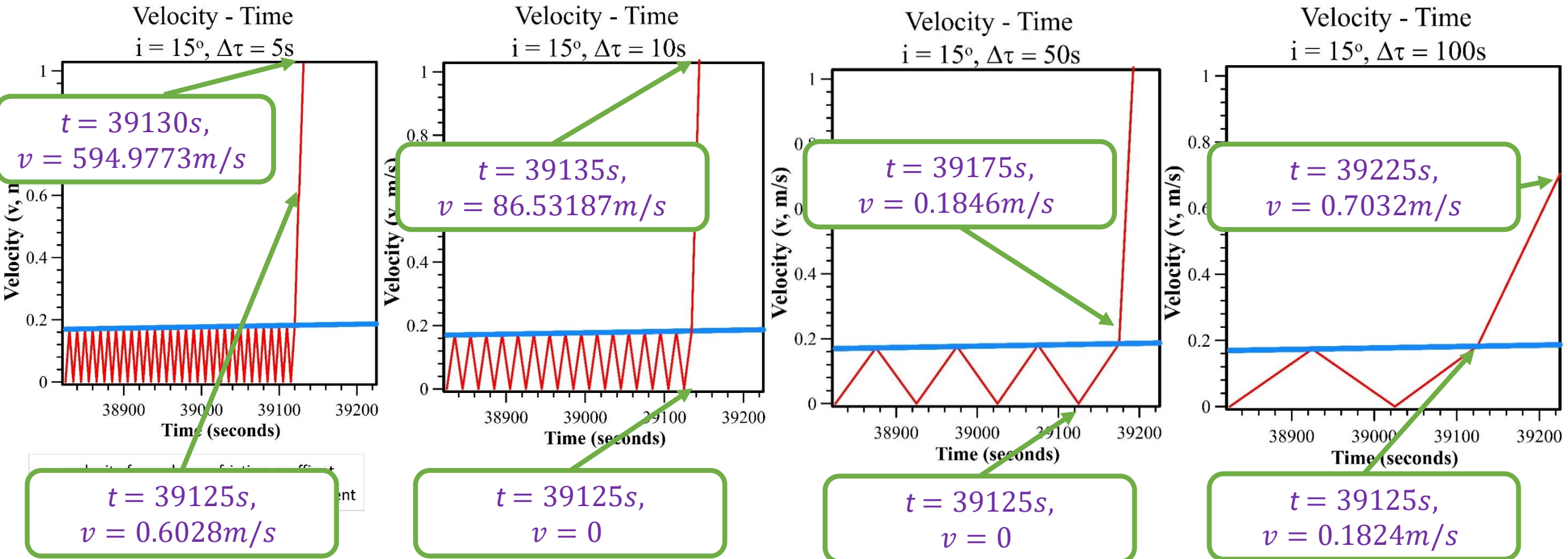
Velocity - Time
 $i = 15^\circ, \Delta\tau = 5s$ Velocity - Time
 $i = 15^\circ, \Delta\tau = 10s$ Velocity - Time
 $i = 15^\circ, \Delta\tau = 50s$ Velocity - Time
 $i = 15^\circ, \Delta\tau = 100s$ 

— velocity from constant friction coefficient
— Velocity from change friction coefficient

Velocity like figure zigzag

Velocity from change friction coefficient is limited by velocity from constant friction coefficient

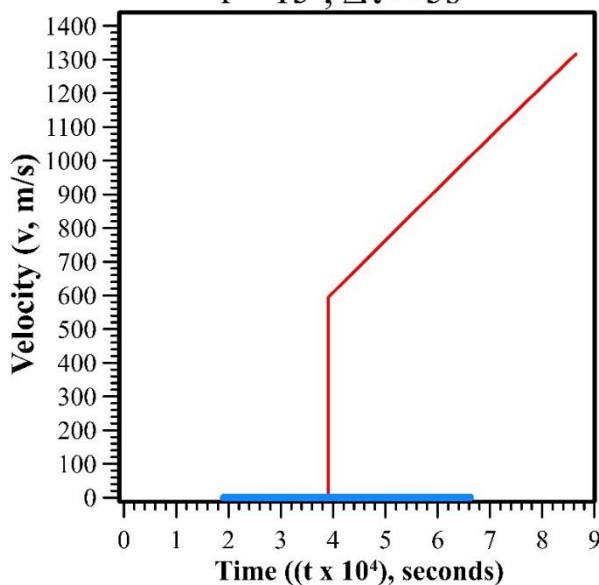
Velocity with different Δt



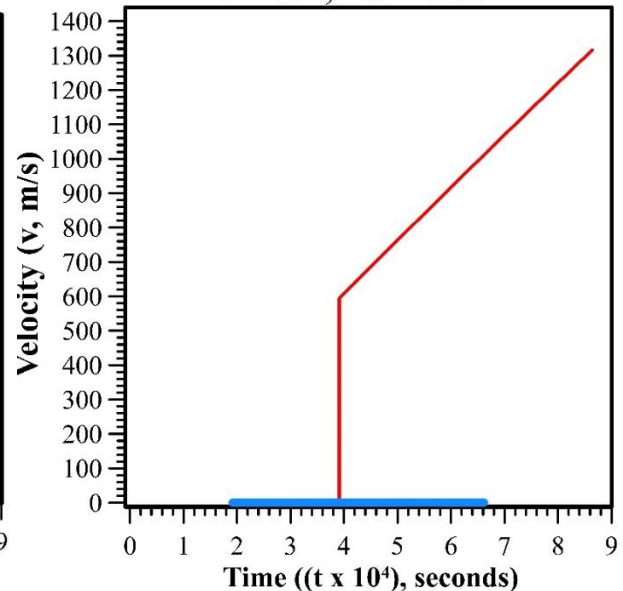
Velocity changes slightly before sudden velocity

Velocity with different Δt

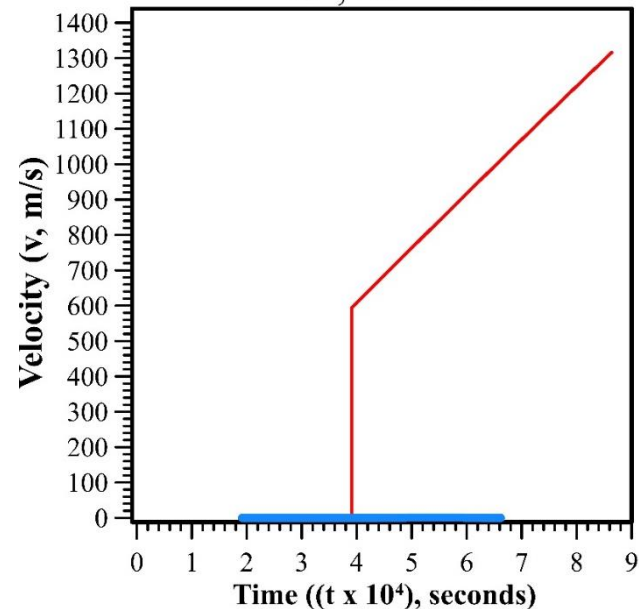
Velocity - Time
 $i = 15^\circ$, $\Delta\tau = 5s$



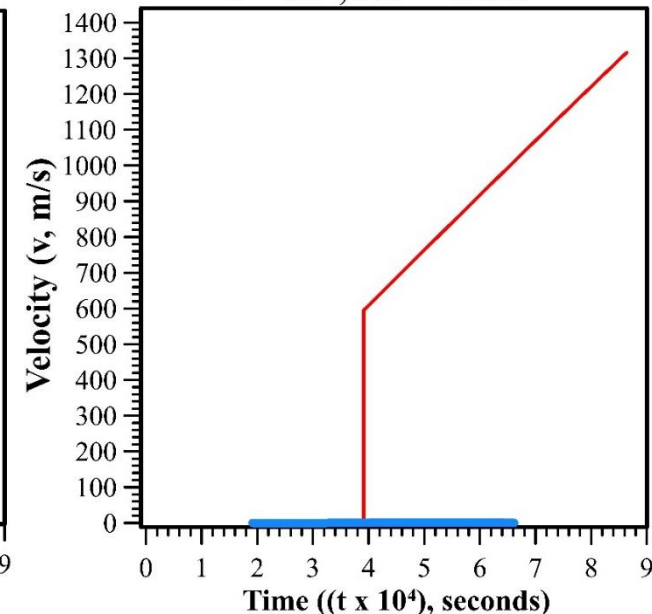
Velocity - Time
 $i = 15^\circ$, $\Delta\tau = 10s$



Velocity - Time
 $i = 15^\circ$, $\Delta\tau = 50s$



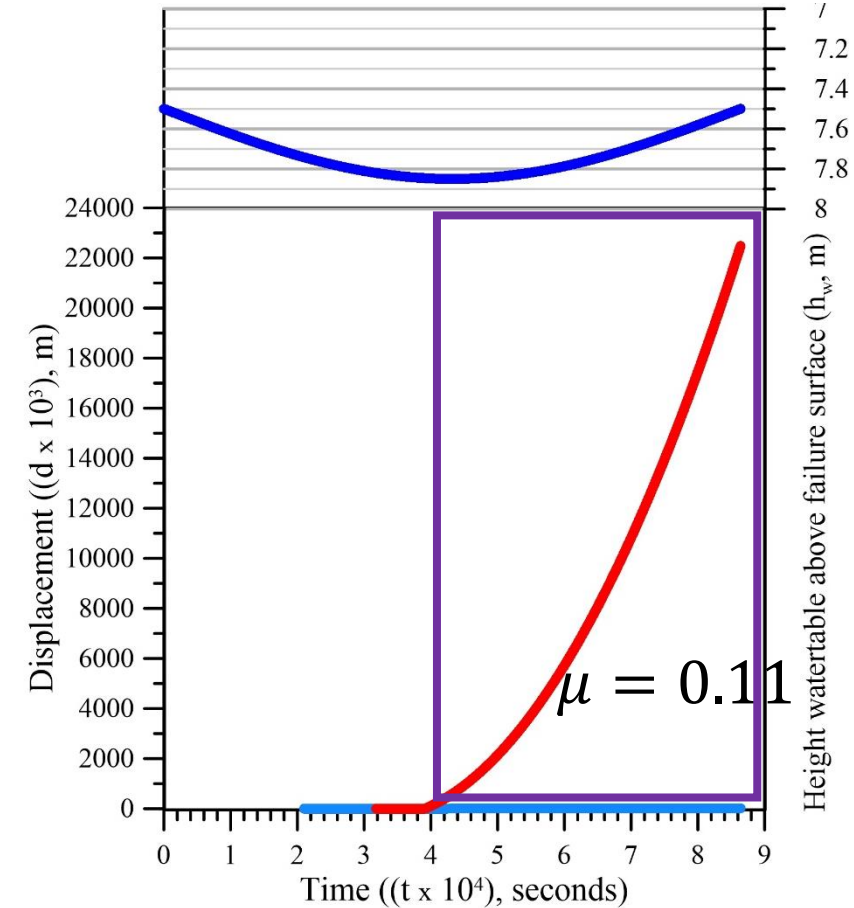
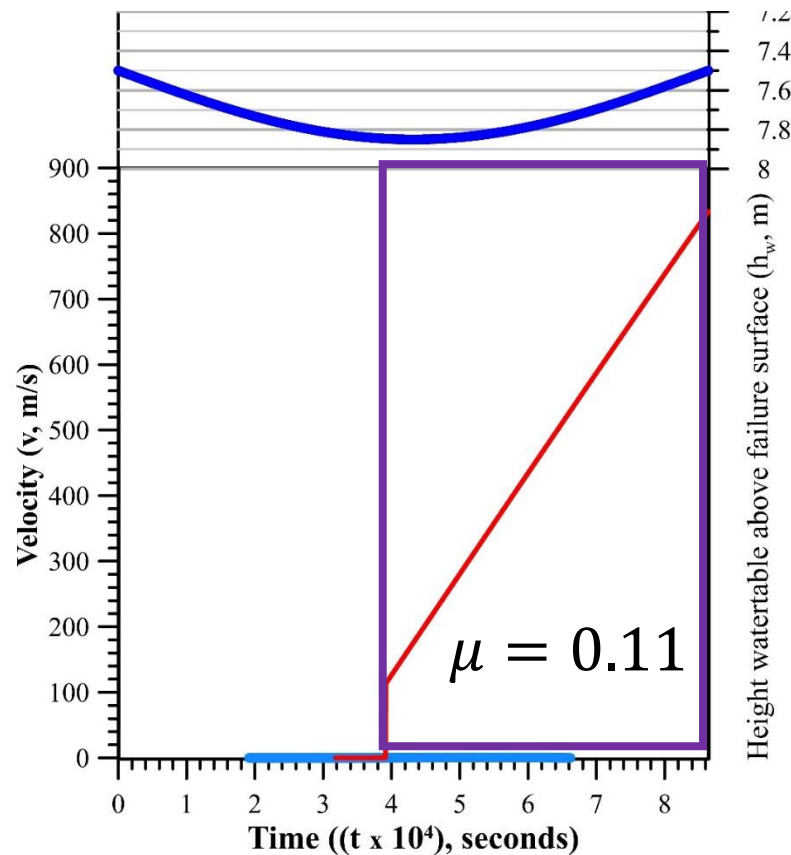
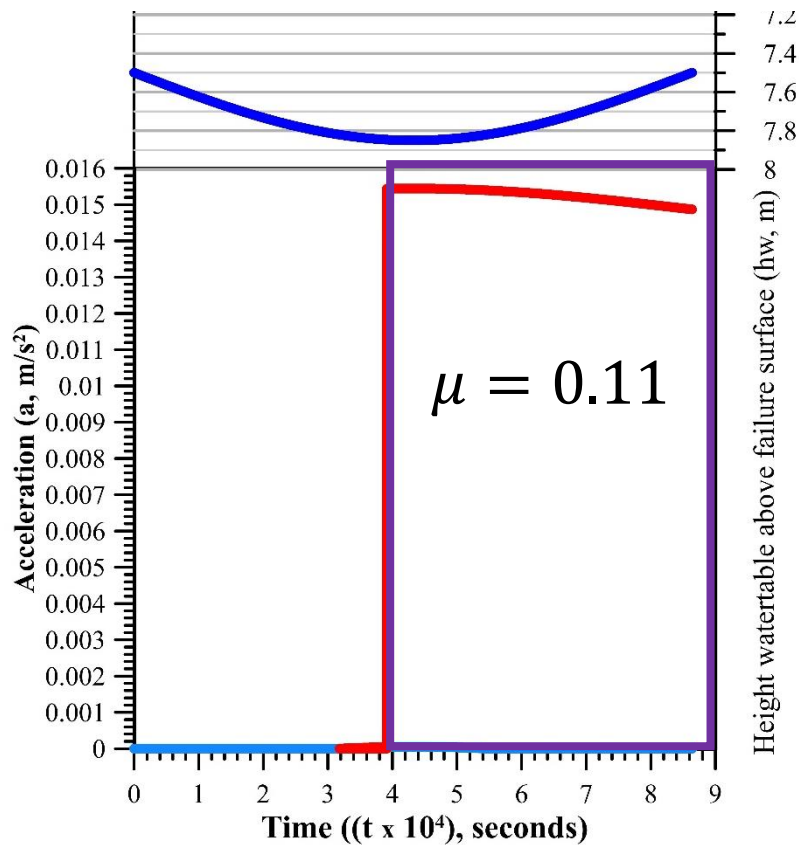
Velocity - Time
 $i = 15^\circ$, $\Delta\tau = 100s$



— velocity from change friction coefficient
— Velocity from constant friction coefficient

Velocity of different Δt is similar

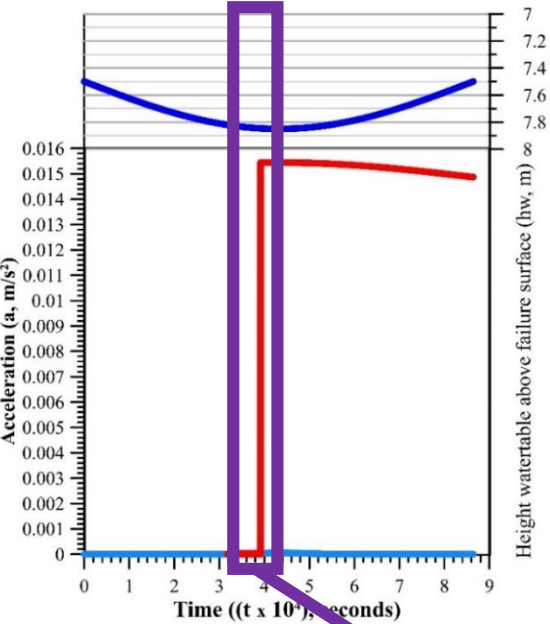
$$i = 15^\circ, h_w = 7.5 \text{ to } 7.85 \text{ m}, \Delta t = 10 \text{ s}$$



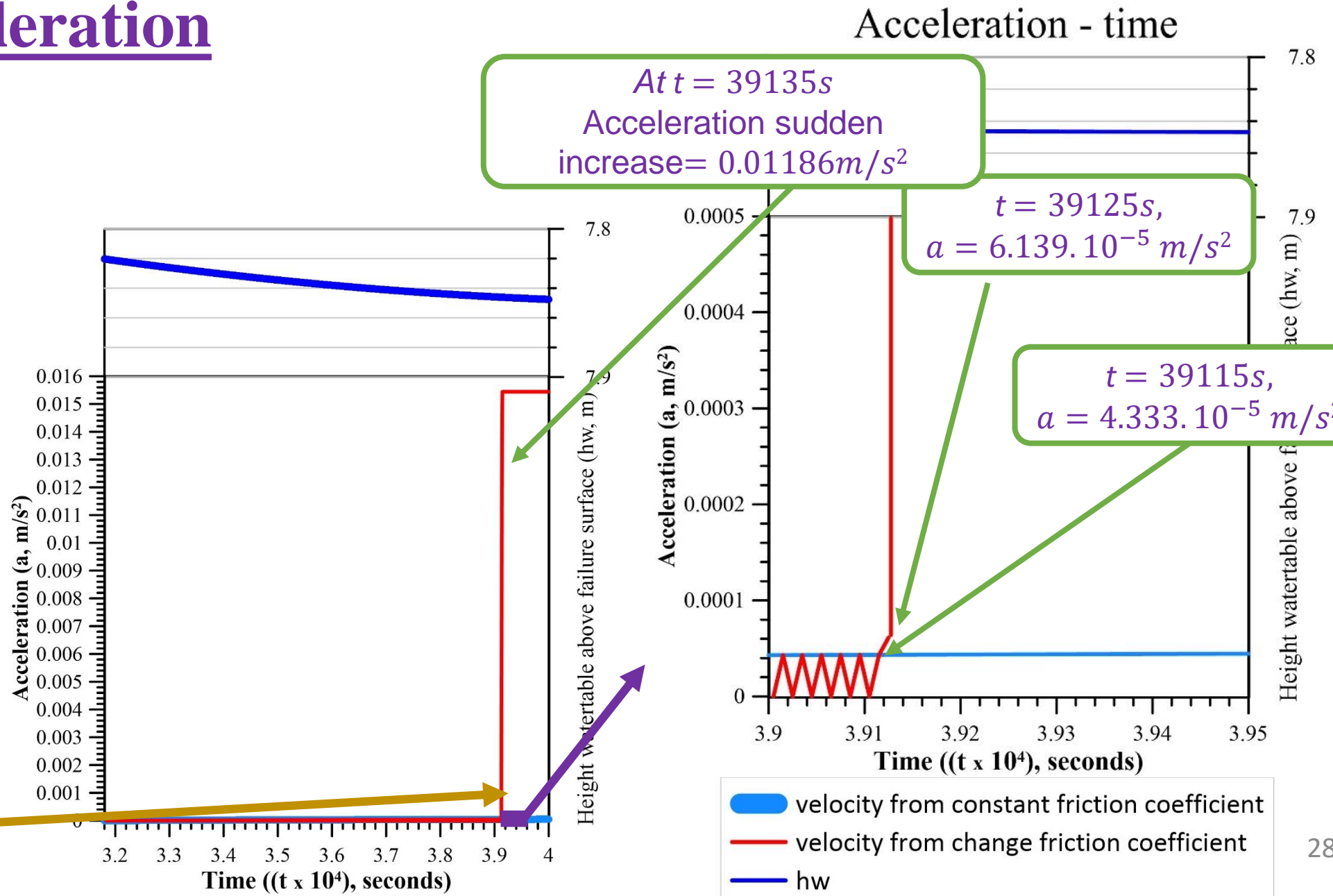
- acceleration from constant friction coefficient
- acceleration from change friction coefficient
- h_w

At $t = 39125 \text{ s}$ with $v \geq 0.19 \text{ m/s}$ then $\mu = 0.11$ The block slides and no affect by height watertable above failure surface

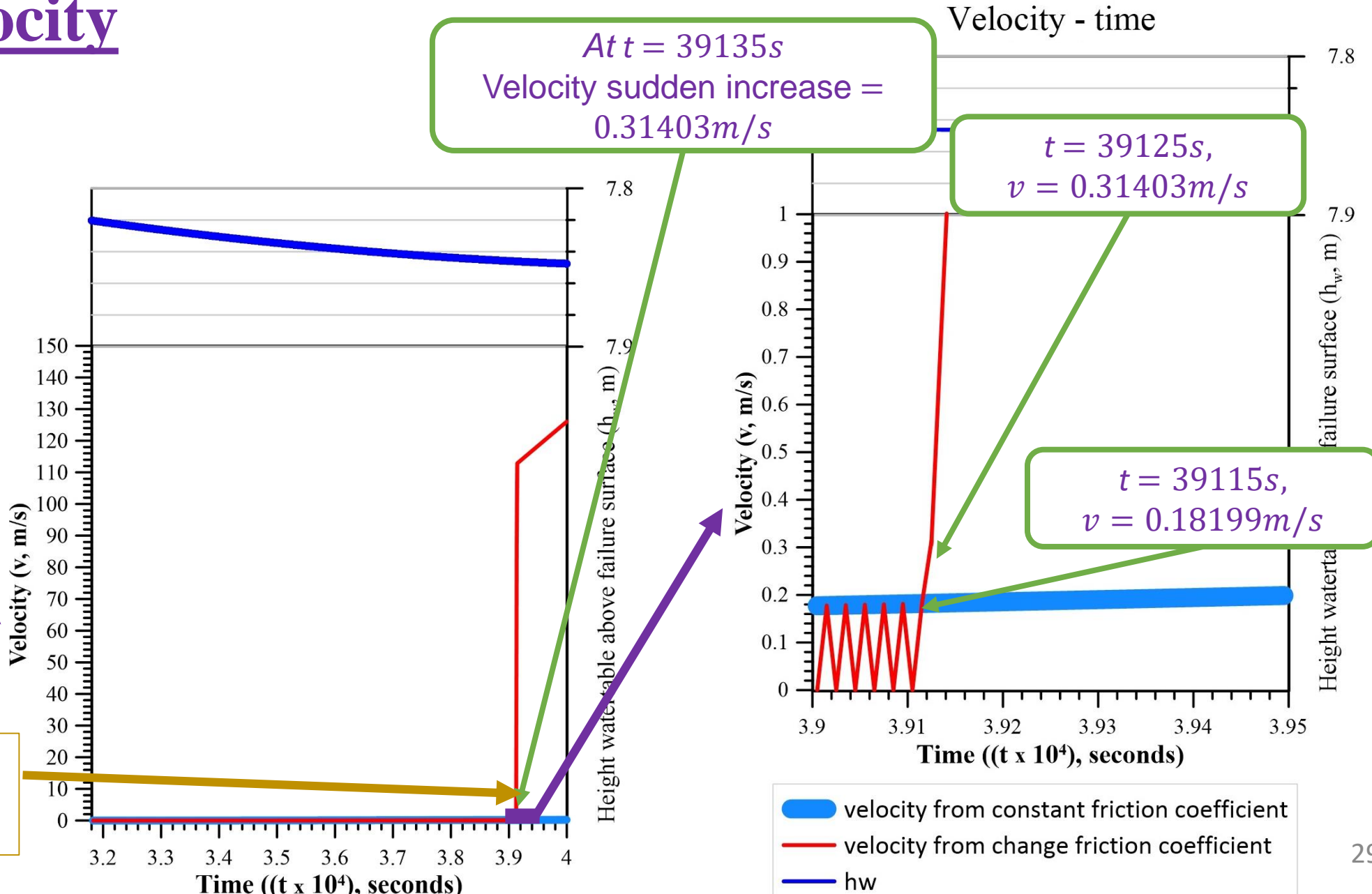
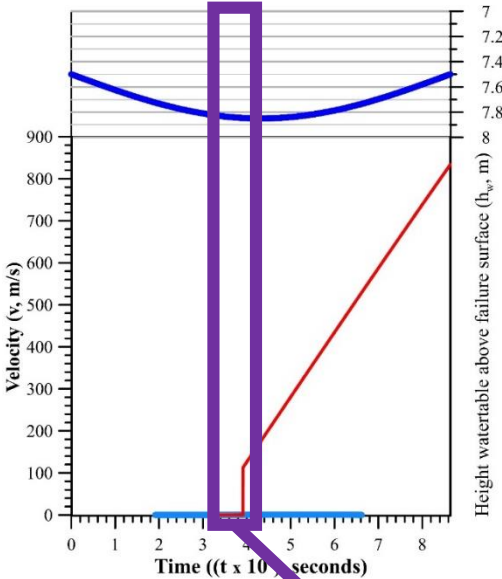
Sudden acceleration



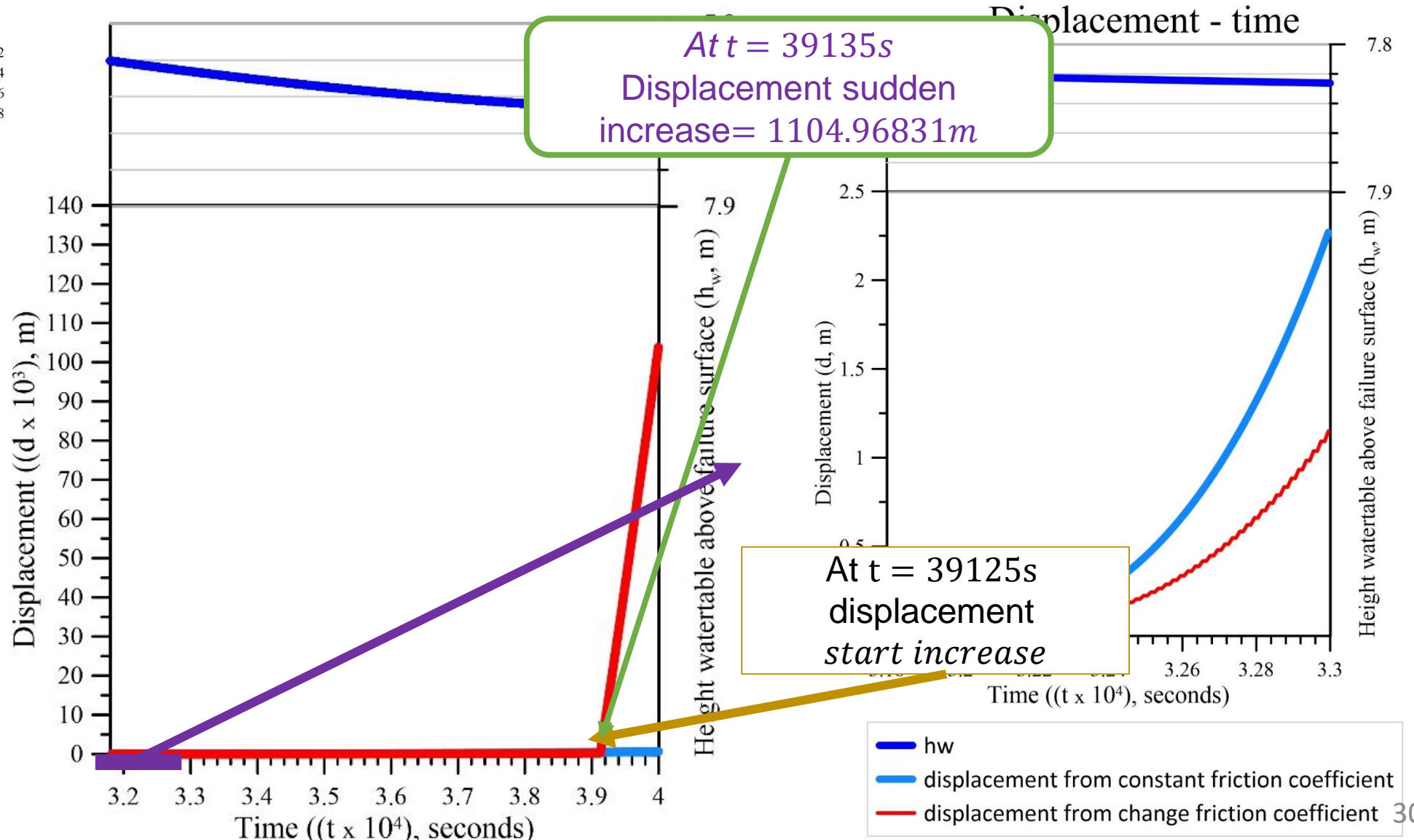
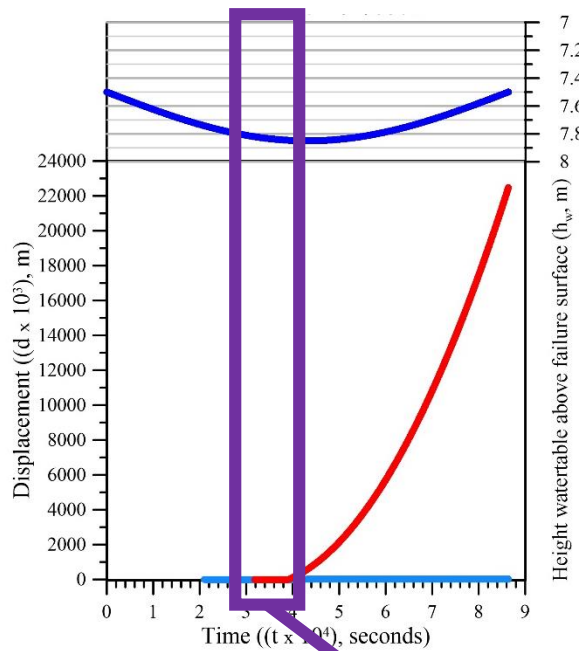
At $t = 39125s$
 acceleration
 start increase
 = $0.00006m/s^2$



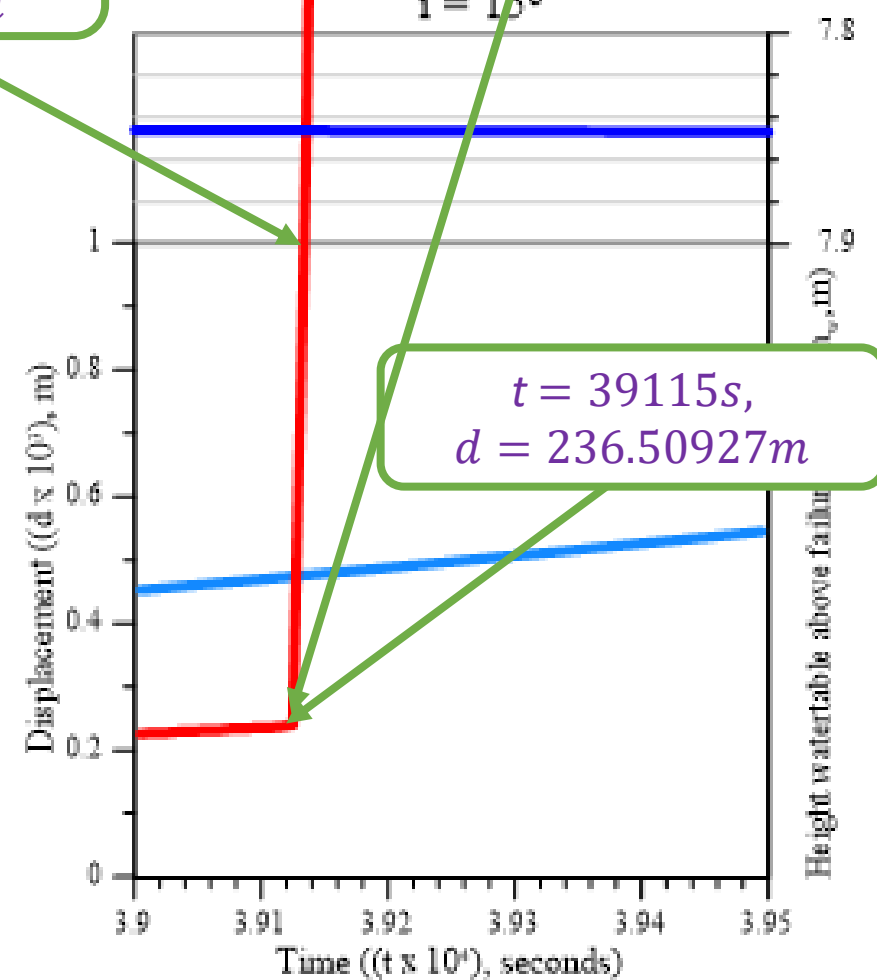
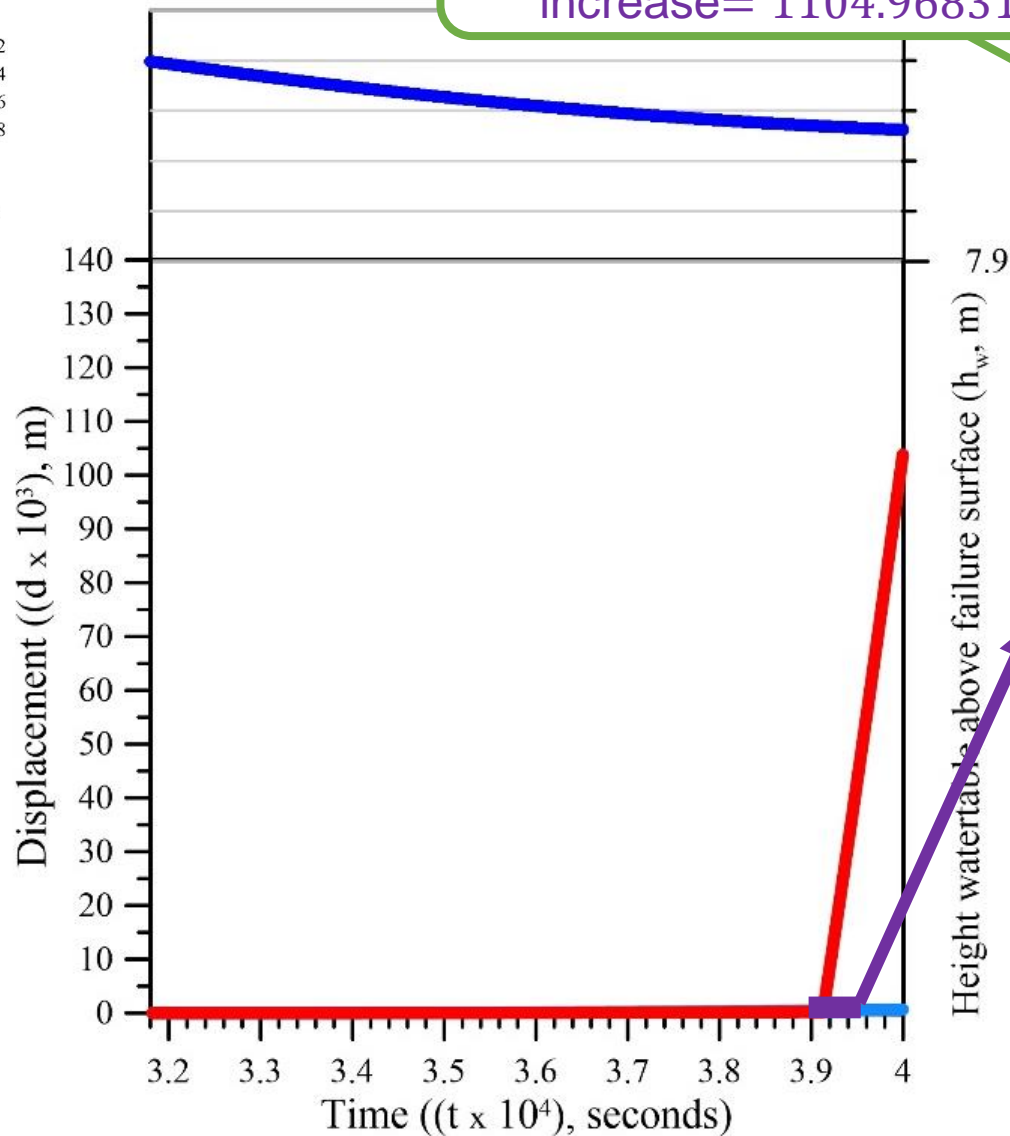
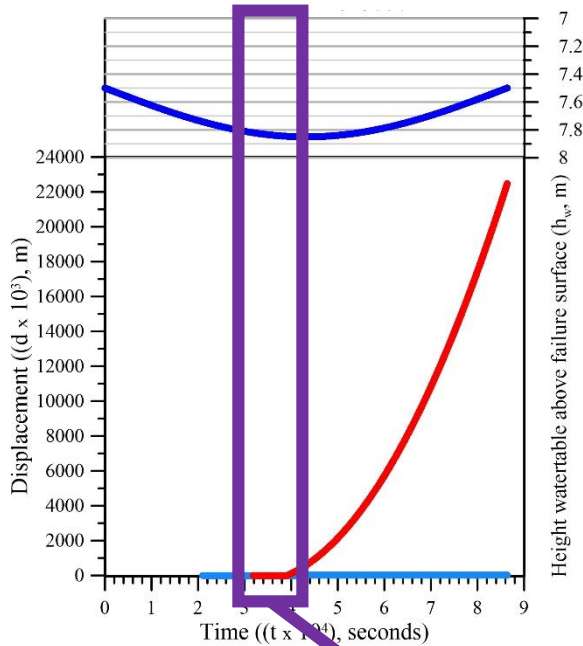
Sudden velocity



Displacement from change $\mu <$ displacement from constant μ



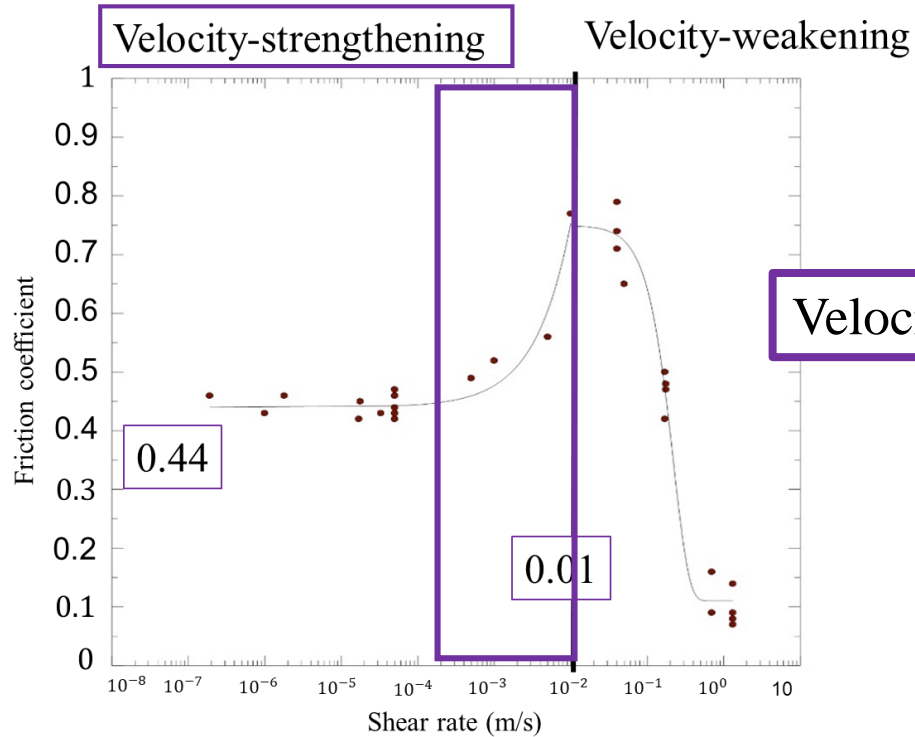
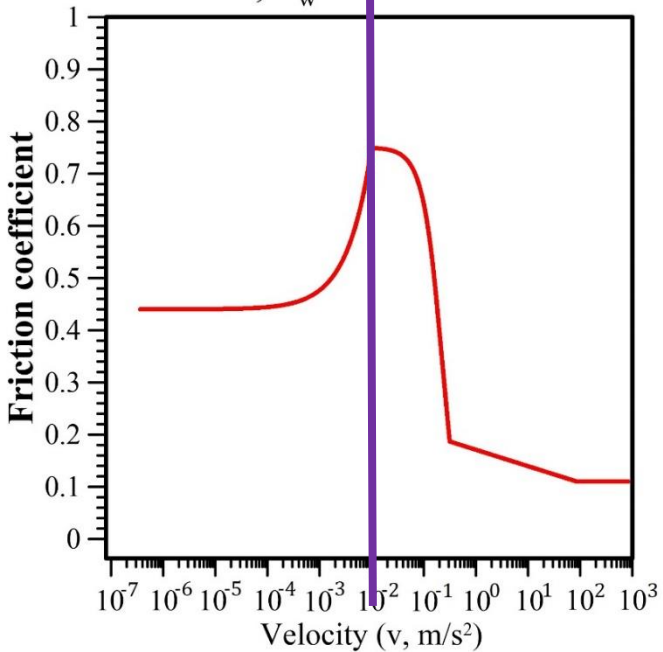
Sudden displacement



- displacement from constant velocity
- displacement from change velocity
- dw

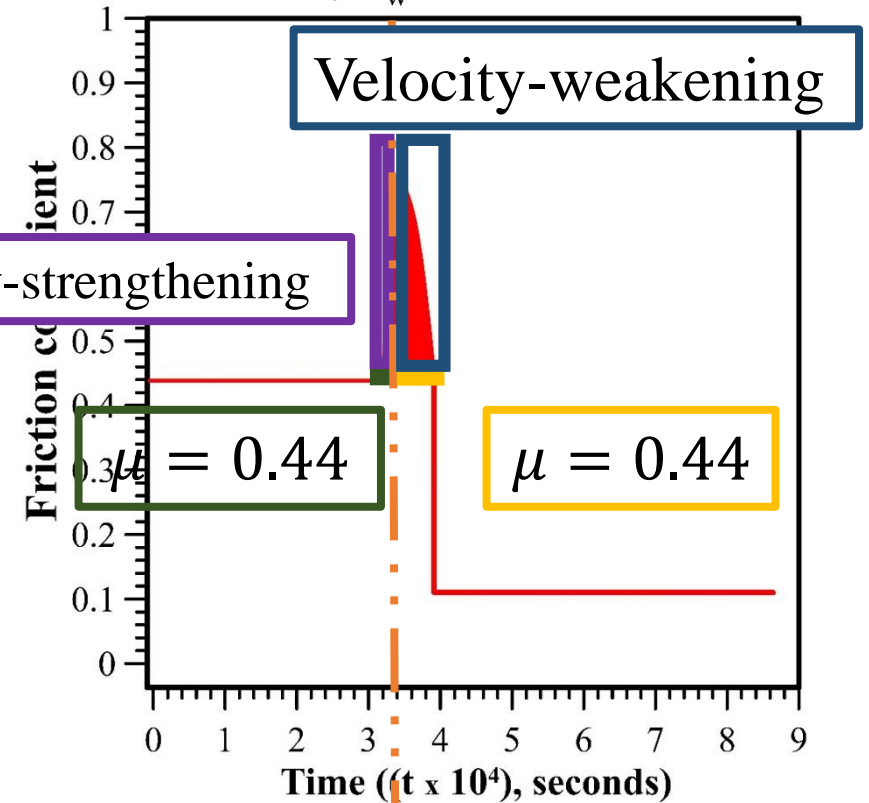
Friction coefficient – Time include 4 part

Friction coefficient - Velocity
 $i = 15^\circ$, $d_w = 7.5$ to 7.85 m



(Ferri et al., 2011)

Friction coefficient - Time
 $i = 15^\circ$, $d_w = 7.5$ to 7.85 m



$t = 33395$ seconds

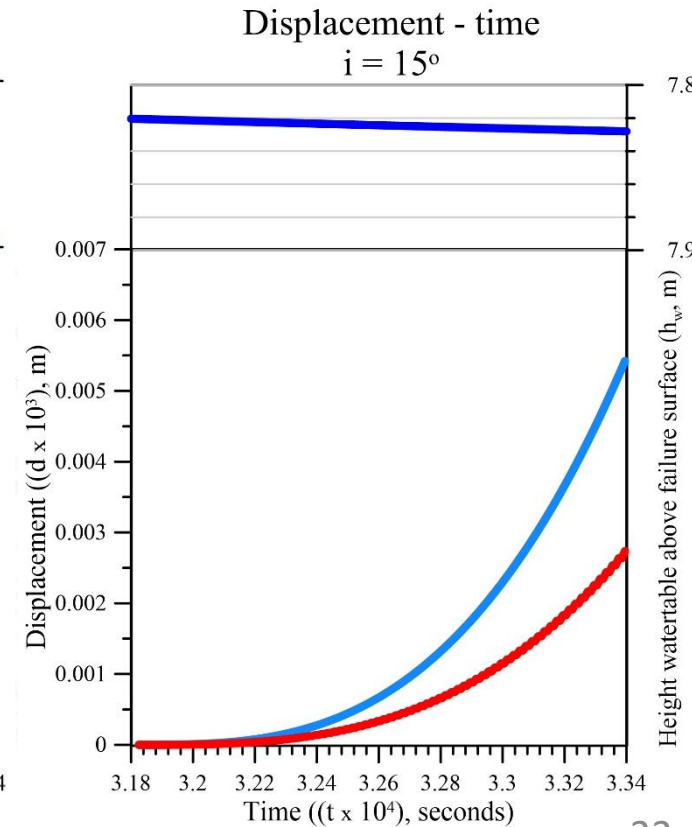
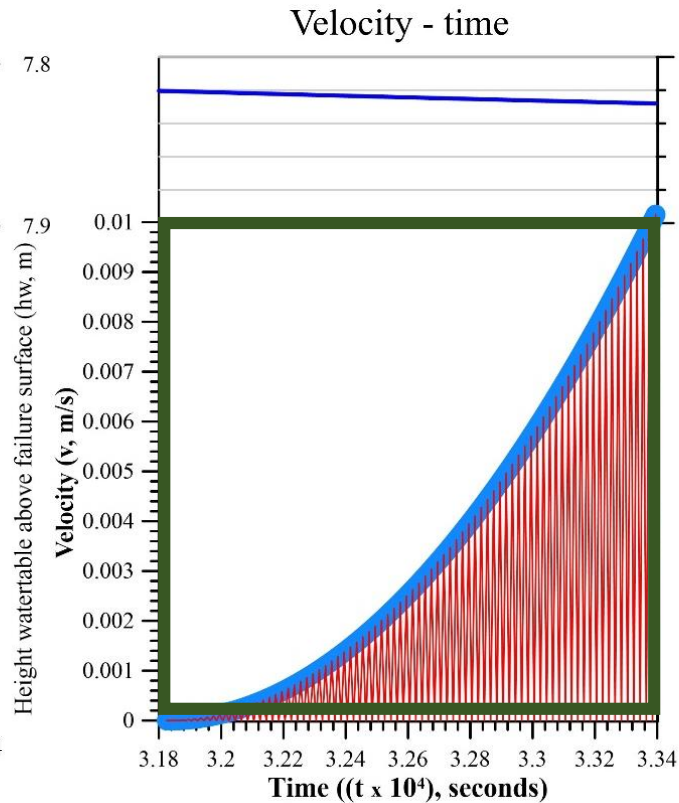
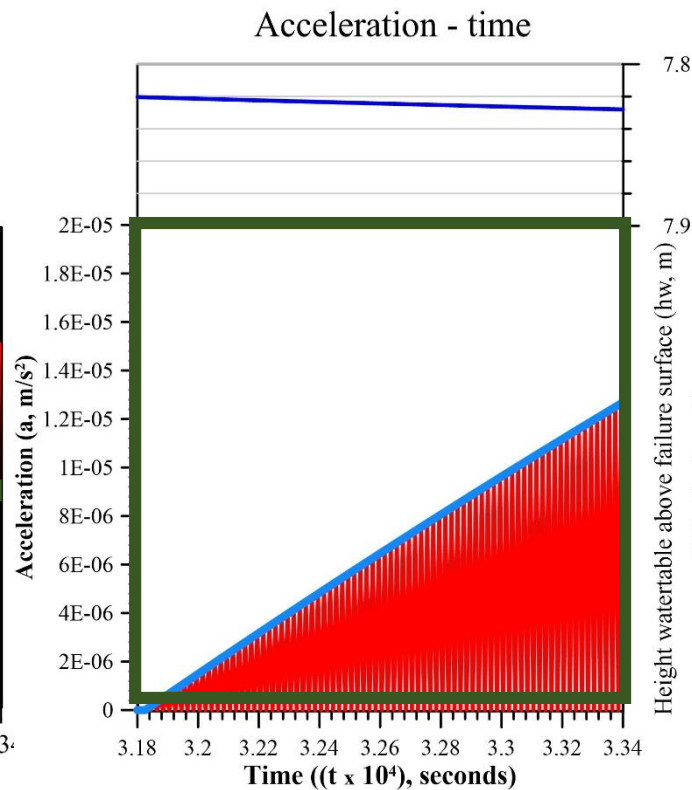
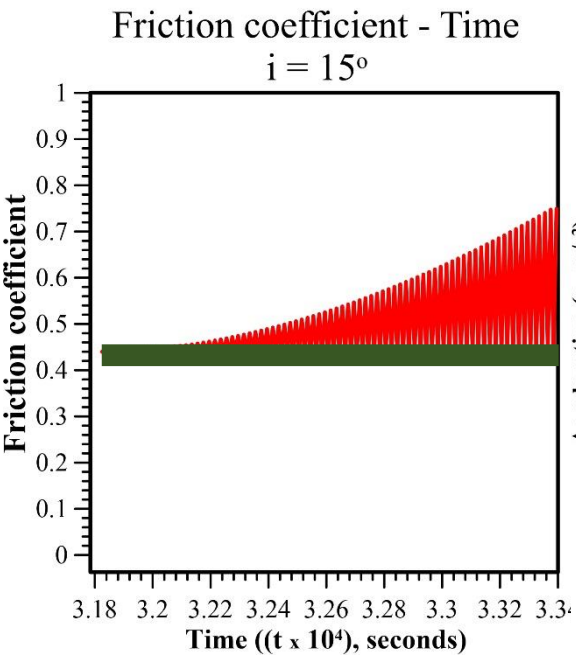
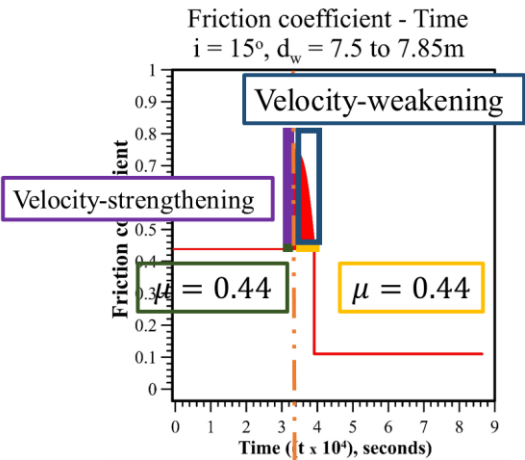
1. Introduction

2. Methodology

3. Results

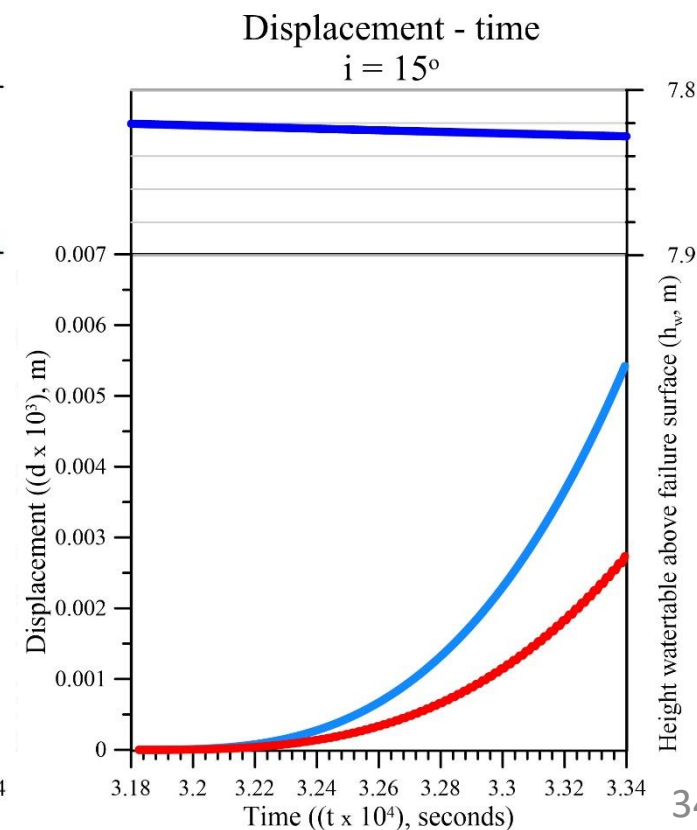
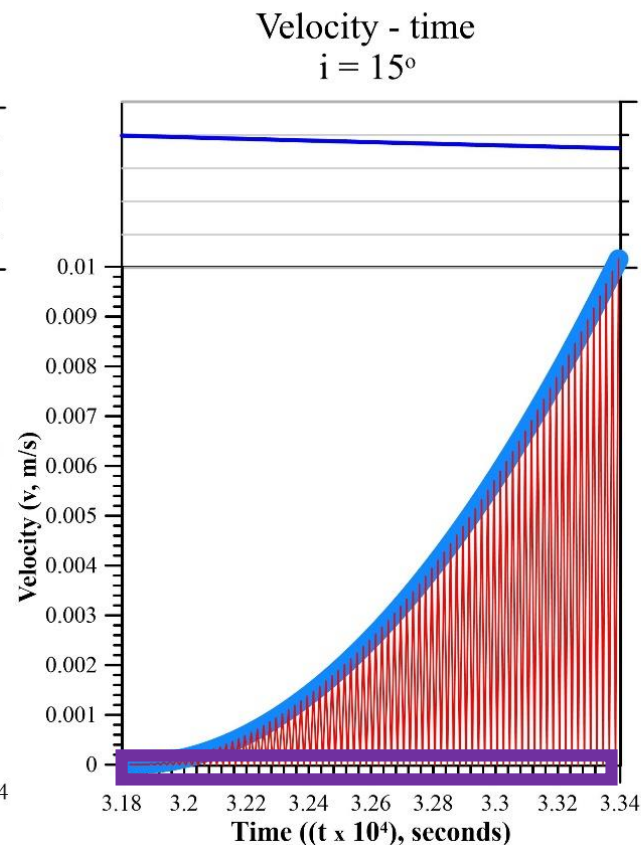
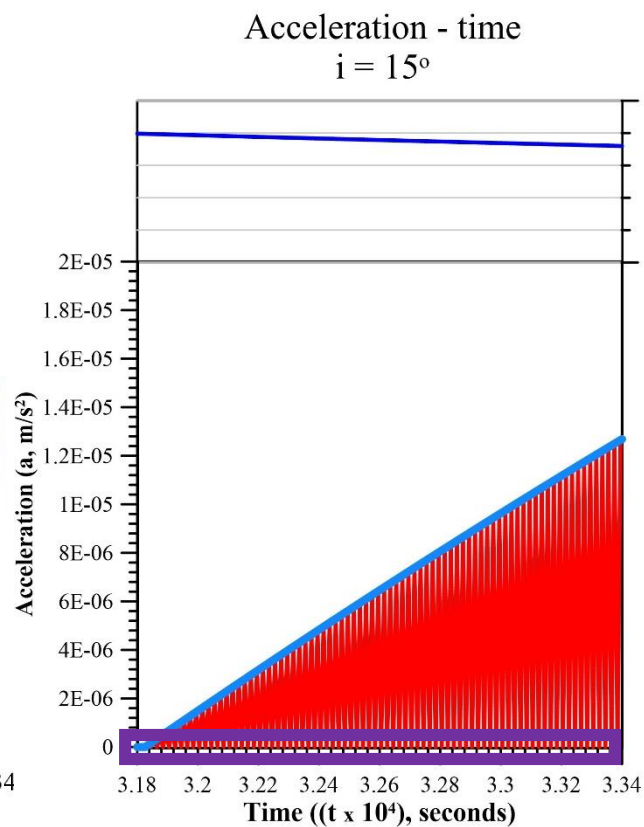
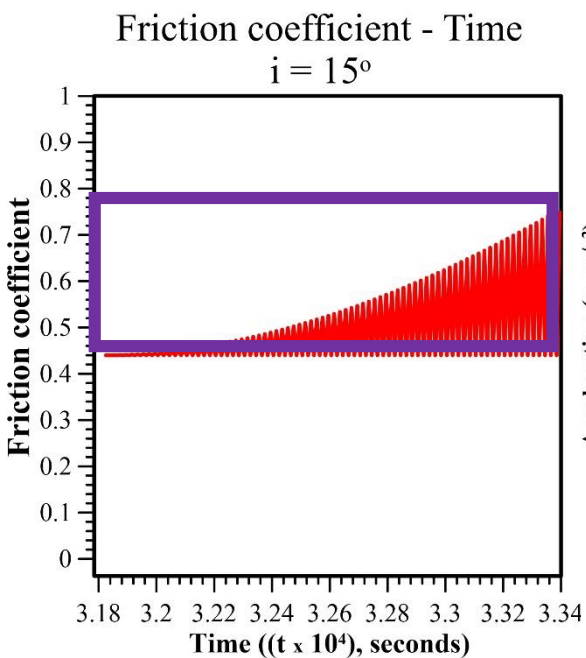
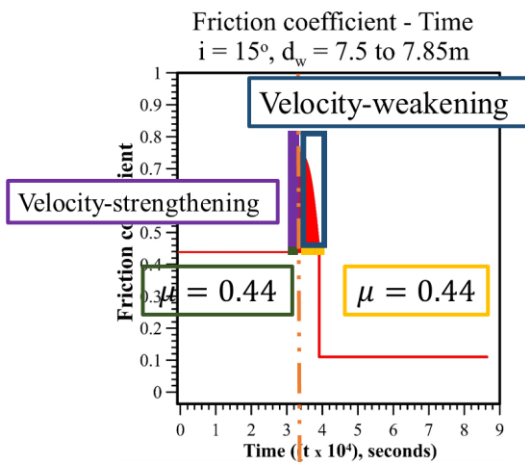
4. Discussion

If $\mu = 0.44$, $a > 0$ and $v > 0$



Velocity-strengthening

If $0.44 < \mu < 0.75$, $a = 0$ and $v = 0$



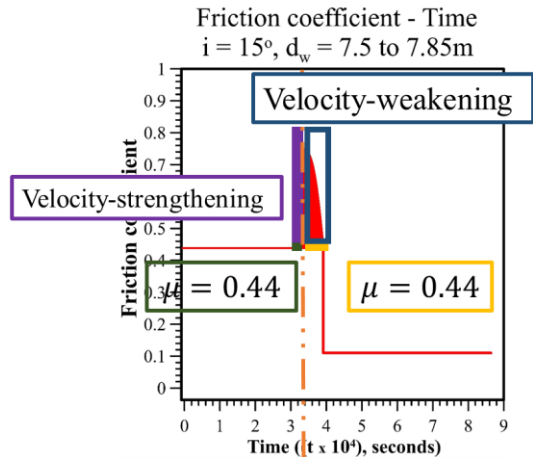
1. Introduction

2. Methodology

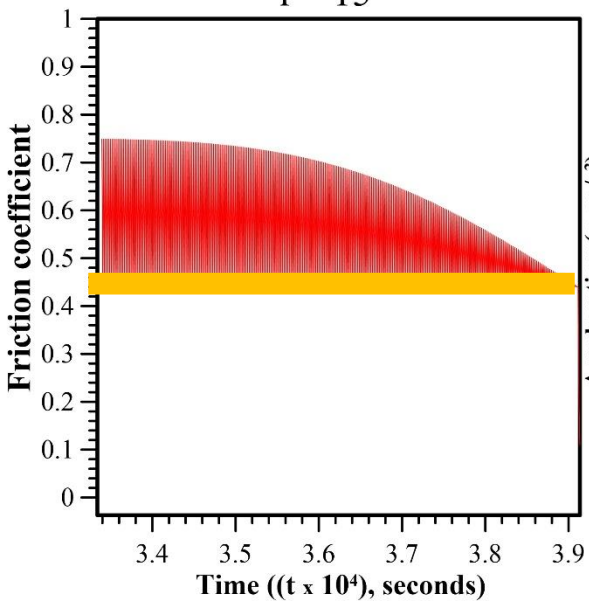
3. Results

4. Discussion

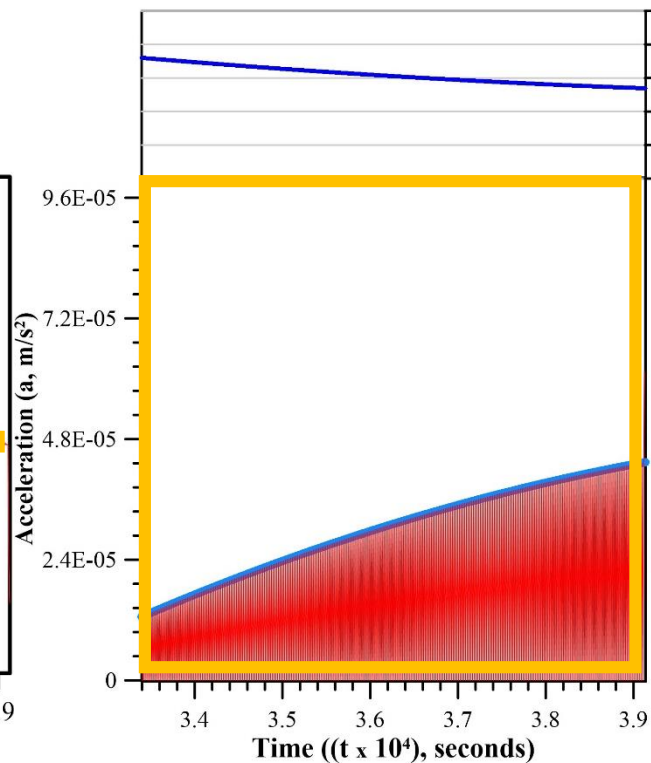
If $\mu = 0.44$, $a > 0$ and $v > 0$



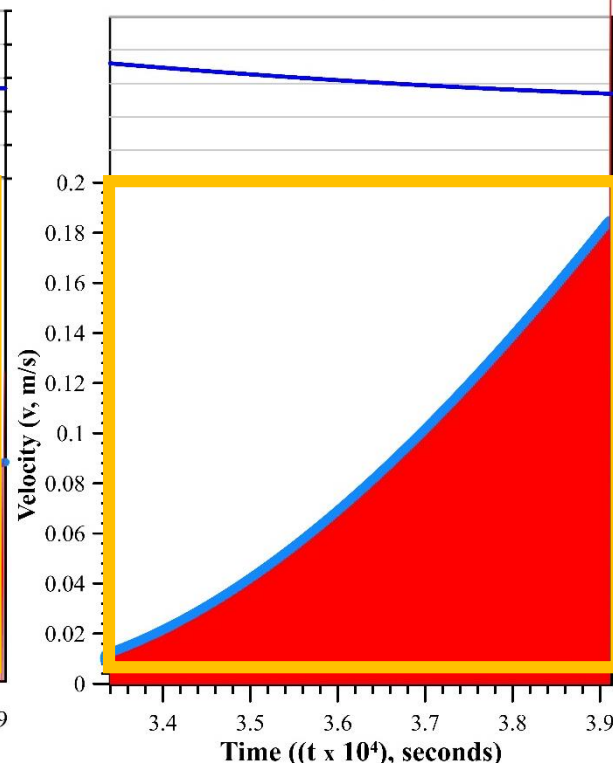
Friction coefficient - Time
 $i = 15^\circ$



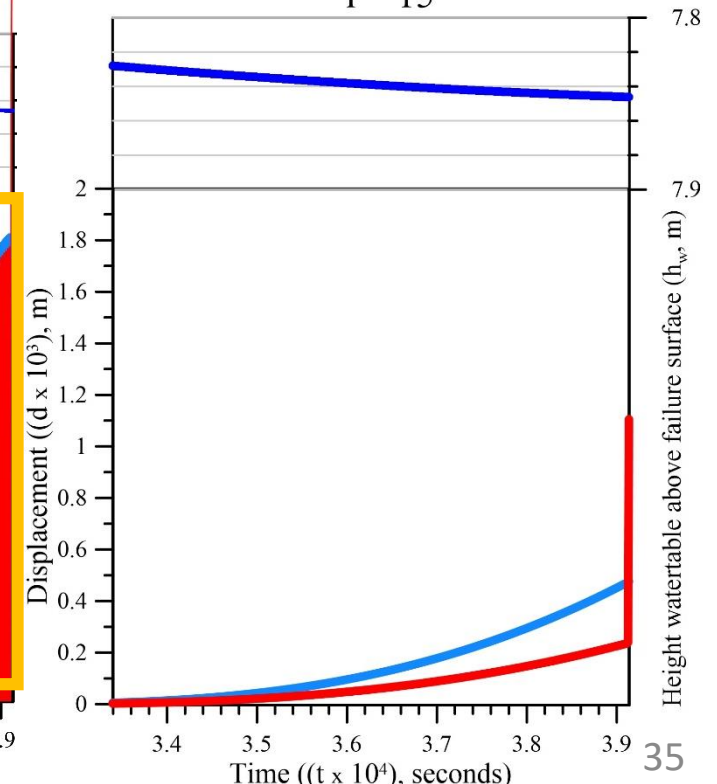
Acceleration - time
 $i = 15^\circ$



Velocity - time
 $i = 15^\circ$

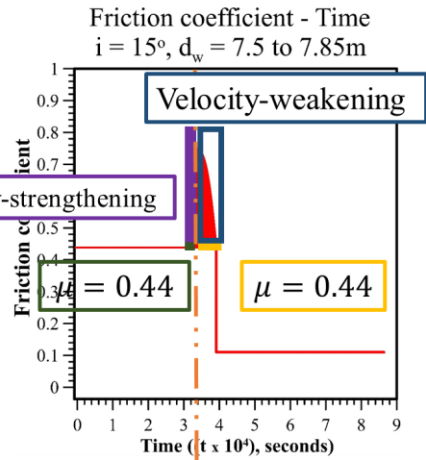


Displacement - time
 $i = 15^\circ$

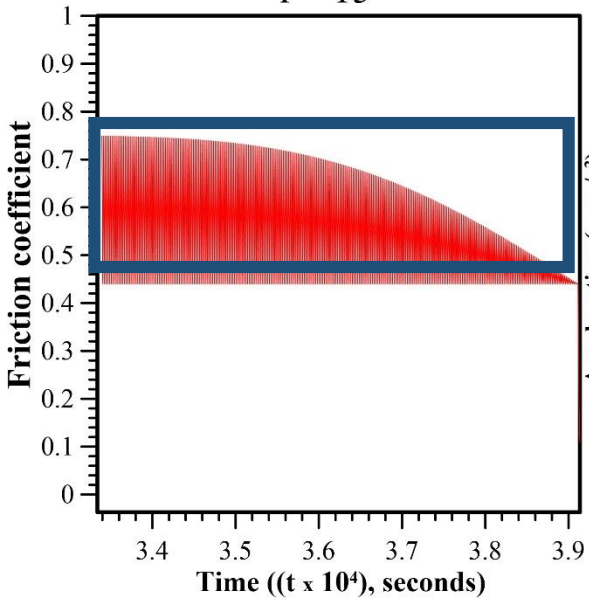


Velocity-weakening

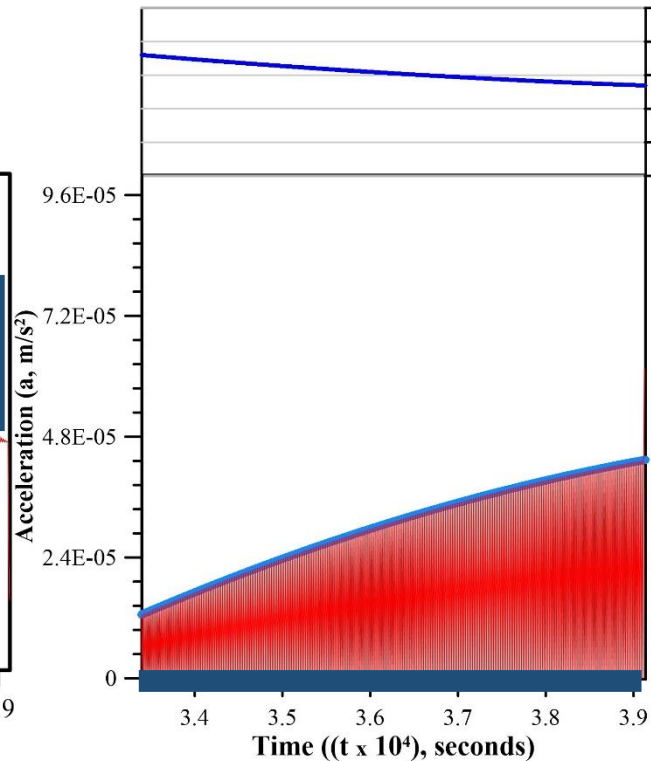
$$0.44 < \mu < 0.75, a = 0 \text{ and } v = 0$$



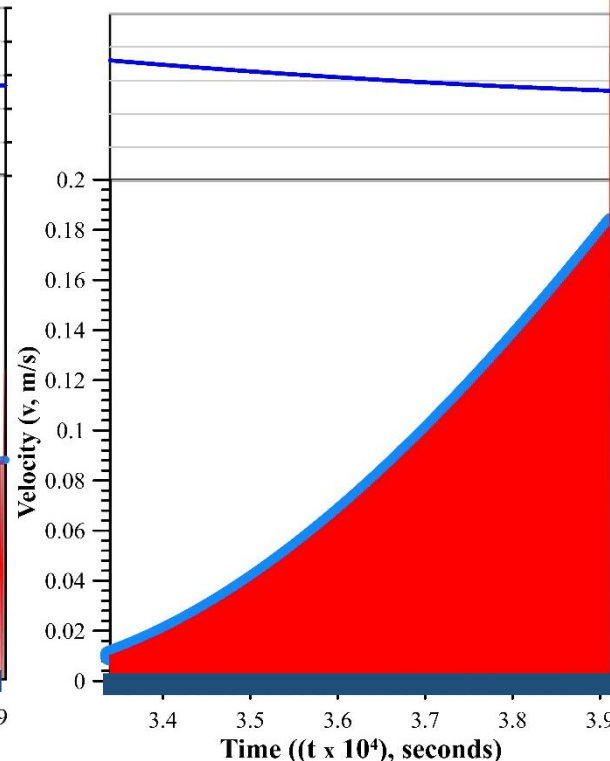
Friction coefficient - Time
 $i = 15^\circ$



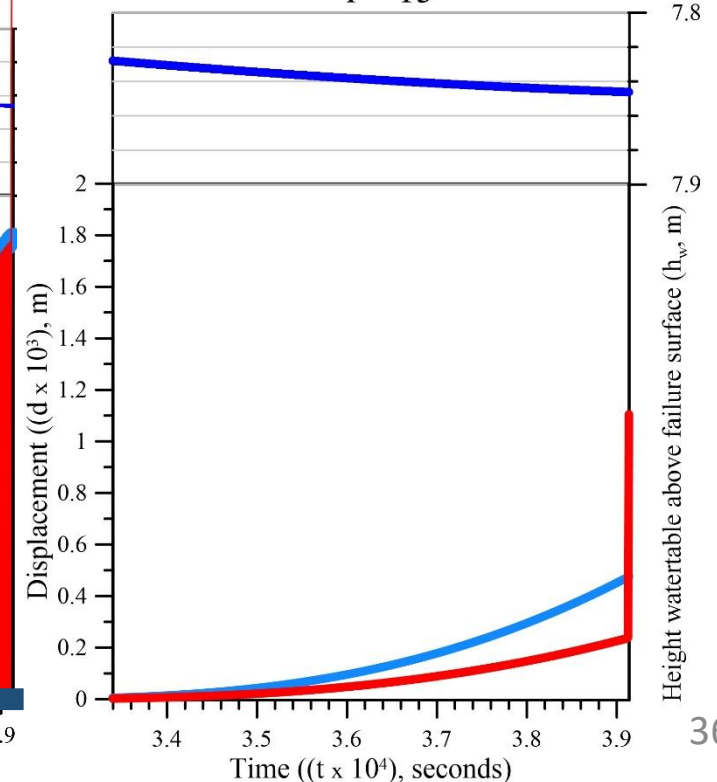
Acceleration - time
 $i = 15^\circ$



Velocity - time
 $i = 15^\circ$

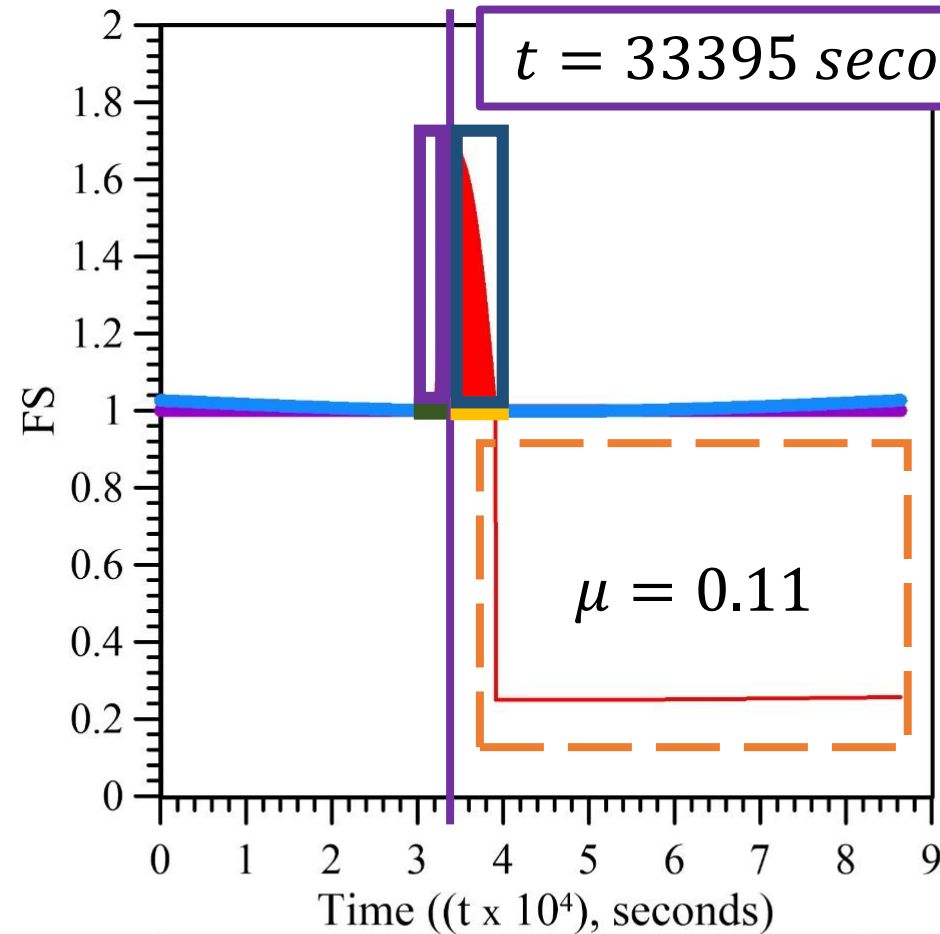


Displacement - time
 $i = 15^\circ$



Fs – time similar Friction coefficient - time

Include 4 part



- FS = 1
- FS from constant friction coefficient
- FS from change friction coefficient

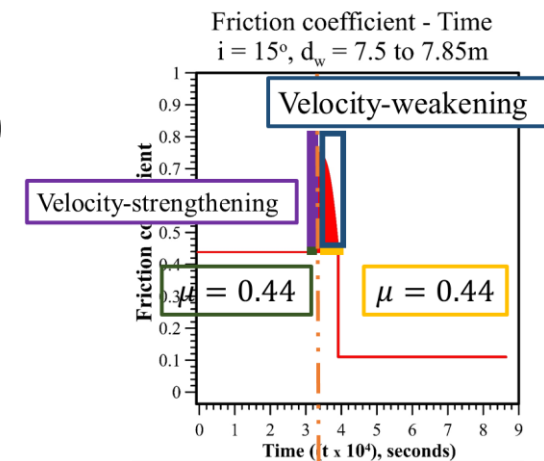
1. Introduction

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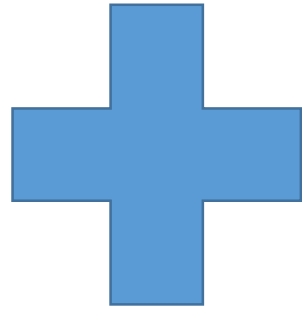
- Most differences Δt have similar results (both acceleration, velocity increase and decrease as shown in figure Zigzag and are limited by acceleration and velocity from constant friction coefficient)
- However, at t with $v \geq 0.19 \text{ m/s}$ then $\mu = 0.11$ so acceleration, velocity, displacement sudden increase. The block slides and no affect by height watertable above failure surface
- when velocity increases, then stops, displacement will increase then horizontal
- In the process of h_w increasing the sinusoid with time, μ also changes continuously according to the figure Zigzag divided into 4 parts:
 - ✓ If $\mu = 0.44$, $a > 0$ and $v > 0$
 - ✓ Velocity-strengthening. If $0.44 < \mu < 0.75$, $a = 0$ and $v = 0$
 - ✓ If $\mu = 0.44$, $a > 0$ and $v > 0$
 - ✓ Velocity-weakening. If $0.44 < \mu < 0.75$, $a = 0$ and $v = 0$



Future works

$v < 0.01m/s$

Origin
condition



Test more
conditions

h_w

i

Time
(2-3 days)

Decrease final
velocity

Results of
experiment

Velocity-dependent
friction

Test again

Simulate Newmark
displacement

Thank you for listening

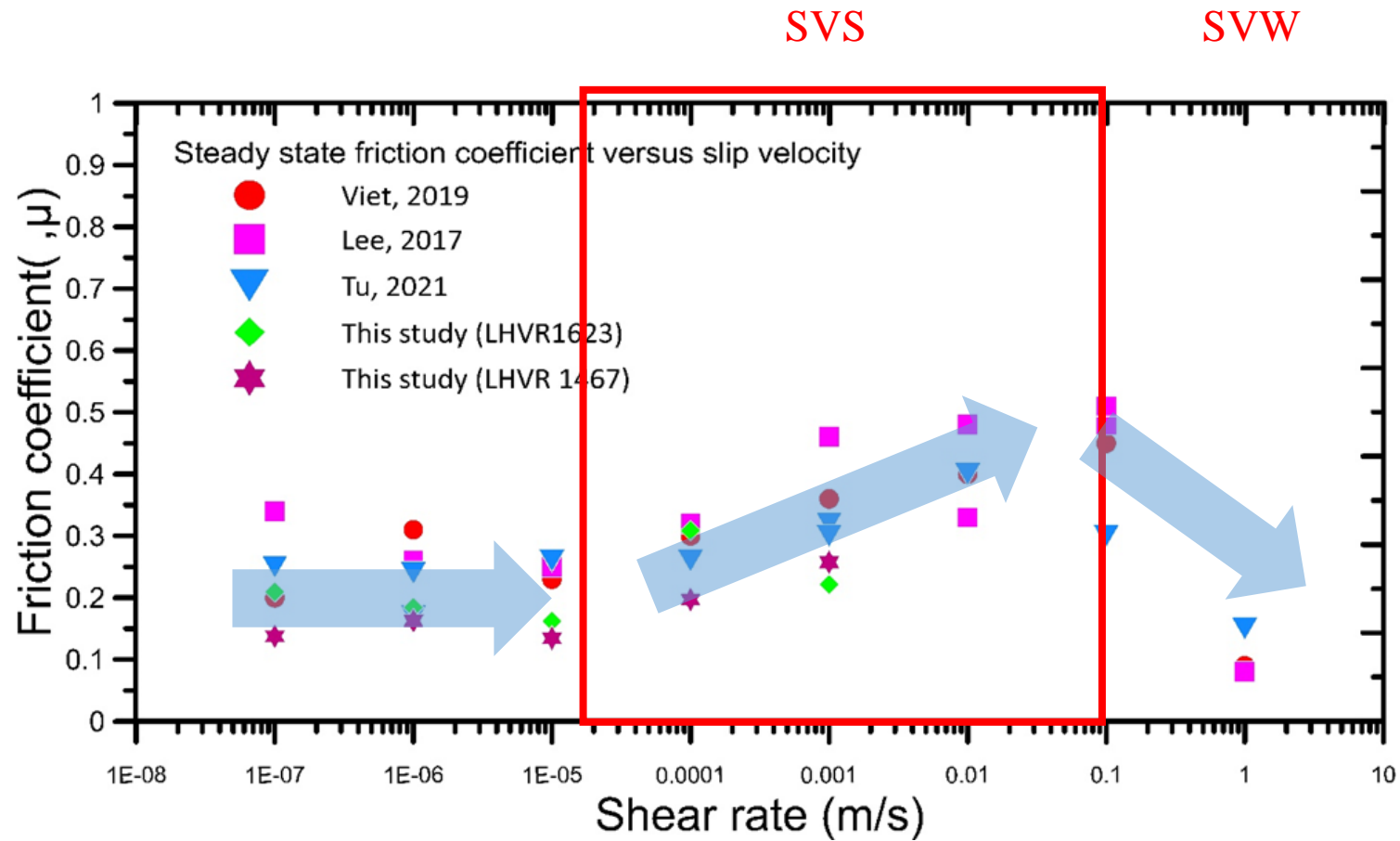


Figure . The steady-state apparent friction coefficients under different slip rates